

# Fundamental interaction studies with nuclear $\beta$ decay

21st Colloque GANIL

Strasbourg, Sept 2019

**Martín González-Alonso**

IFIC, Univ. of Valencia



**IFIC**  
INSTITUT DE FÍSICA  
CORPUSCULAR



EXCELENCIA  
SEVERO  
OCHOA

# The search for 'New Physics'

## Standard Model

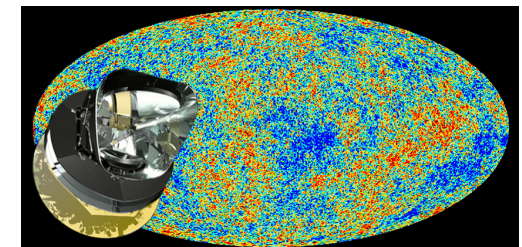
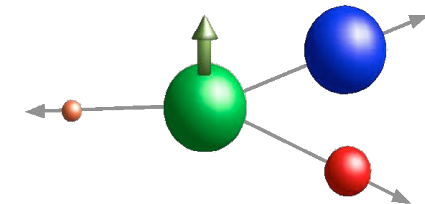
	I	II	III	
mass→	2.4 MeV	1.27 GeV	171.2 GeV	0
charge→	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0
spin→	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
name→	<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>γ</b> photon
				<b>+Higgs!</b>
Quarks				
	4.8 MeV	104 MeV	4.2 GeV	0
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	<b>g</b> gluon
	<2.2 eV	<0.17 MeV	<15.5 MeV	91.2 GeV
	0	0	0	0
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
	<b>ν<sub>e</sub></b> electron neutrino	<b>ν<sub>μ</sub></b> muon neutrino	<b>ν<sub>τ</sub></b> tau neutrino	<b>Z</b> weak force
Leptons				
	0.511 MeV	105.7 MeV	1.777 GeV	80.4 GeV
	-1	-1	-1	$\pm 1$
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1
	<b>e</b> electron	<b>μ</b> muon	<b>τ</b> tau	<b>W</b> weak force

**NEW PHYSICS** : a new theory that completes the SM and solves (at least some of) the current puzzles.

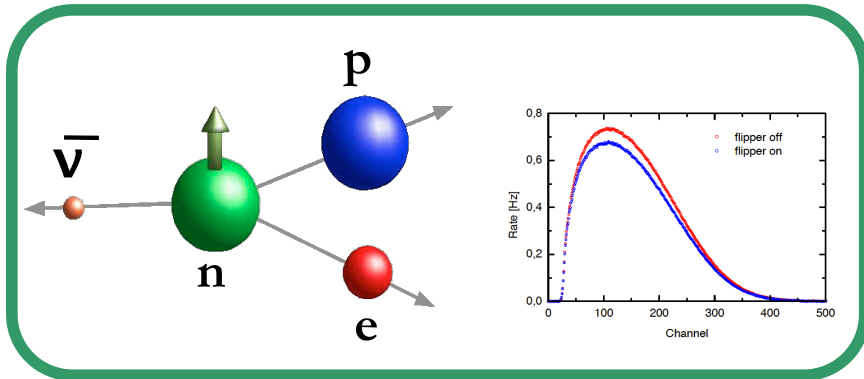
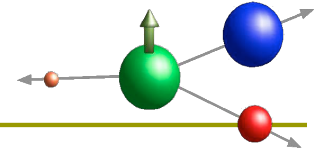


## New Physics experimental searches...

- Energy frontier → LHC, ...
- Intensity frontier → Nuclear physics, muon, ...
- Cosmic frontier → Planck, ...



# New Physics searches with $\beta$ decays

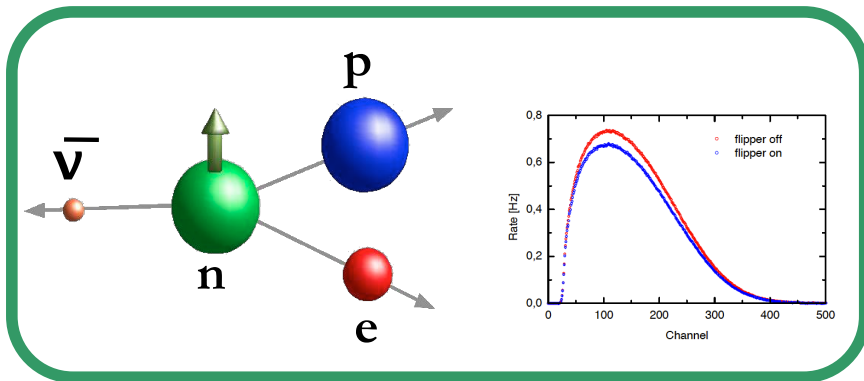
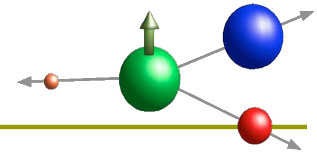


Precise data  
+  
Precise SM predictions

$$[V_{ud} = 0.97416(21)!!!]$$

[Hardy & Towner'15]

# New Physics searches with $\beta$ decays



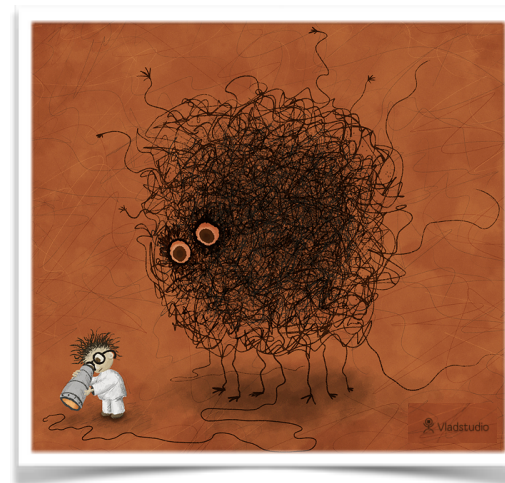
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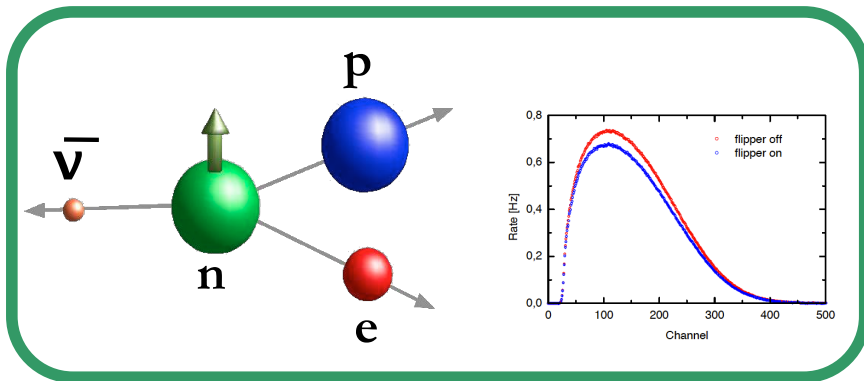
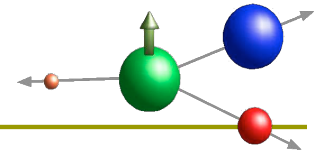
## Implications for New Physics?

- **Specific model;** *Beg et al. (1977), Barbieri et al. (1985), Marciano & Sirlin (1987), Hagiwara et al. (1995), Kurylov & Ramsey-Musolf (2002), Marciano (2007), Bauman et al. (2012), ...*
- **Something more model-indep? EFTs!**





# New Physics searches with $\beta$ decays



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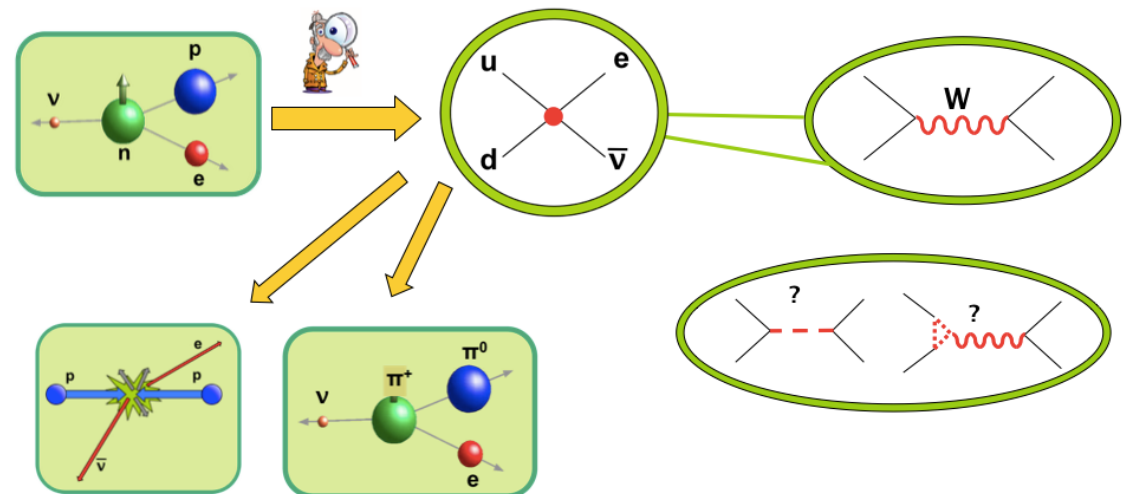
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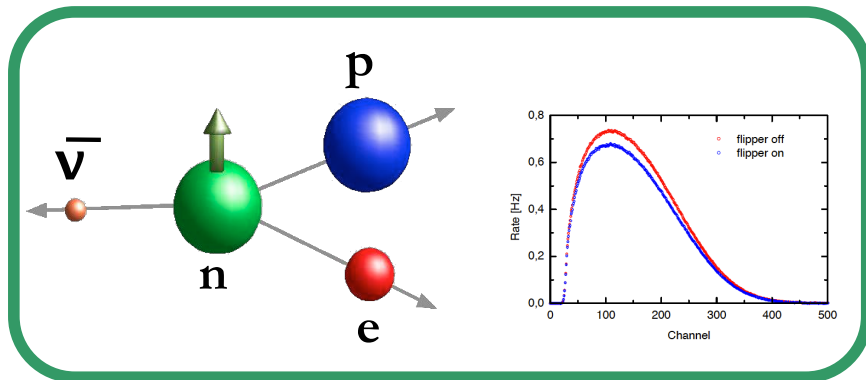
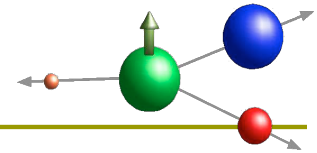
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## Competitive probes?

- **Other low-E searches**
- **High-E (LHC!!)**



# New Physics searches with $\beta$ decays



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+  
Precise SM predictions

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[Hardy & Towner'15]

## Implications for New Physics?

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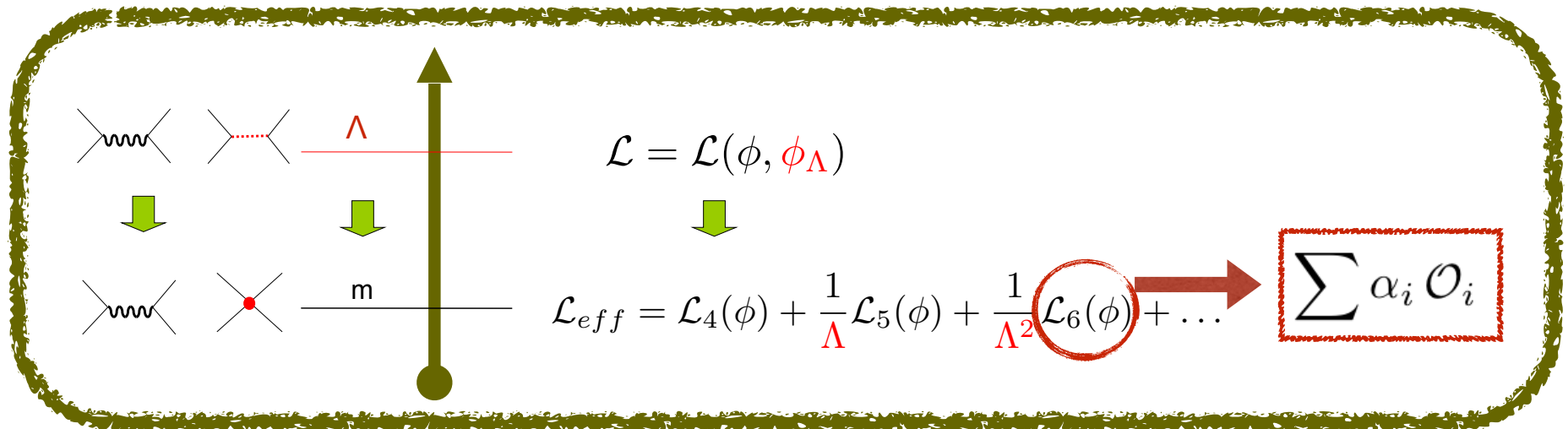
- **Other low-E searches**
- **High-E (LHC!!)**

Very active field!

**["Recent" review:**  
MGA, O. Naviliat Cuncic, N. Severijns,  
Prog. Part. Nucl. Phys. 104 (2019) 165-223]

... outdated a few months afterwards!

# What's an EFT?



$\alpha_i$  : Wilson coefficients.

$$\frac{\alpha_6^{(i)}}{\Lambda^2} = f_i(g_{NP}, M_{NP})$$

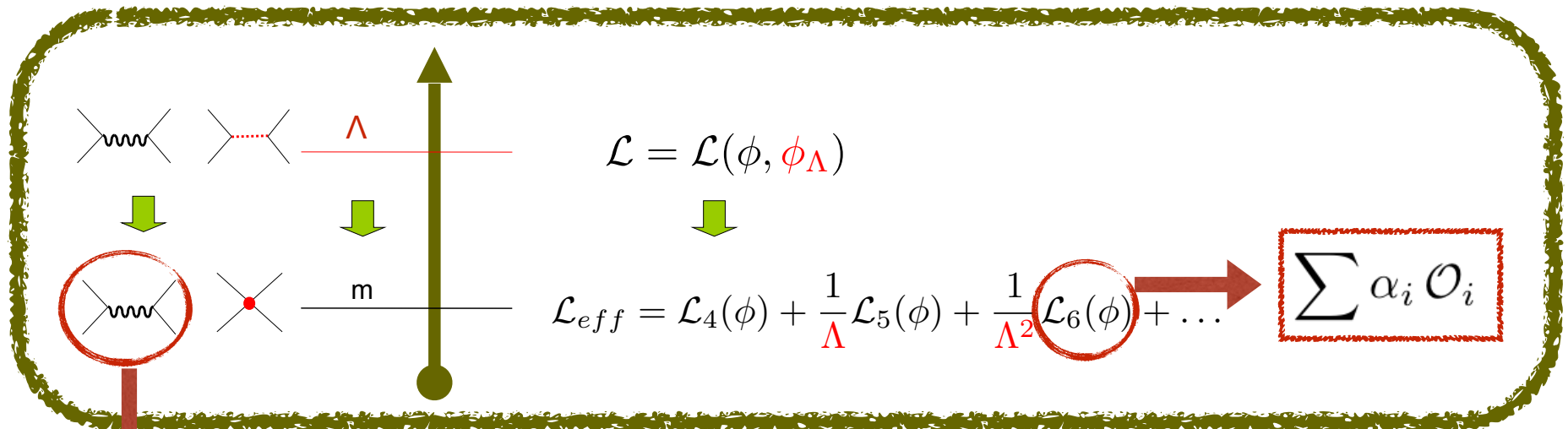
Effective Field Theory = Fields + Symmetries

- nuclei, e,  $\nu$
- hadrons, e,  $\nu$
- q, u, d, l, e
- W, Z,  $\gamma$ , g
- ...

- Lorentz
- QED
- SU(2) x U(1)
- Flavour sym?
- B, L;

Not assumption independent!

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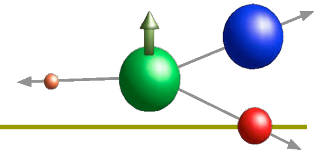
$$-\frac{4G_F}{\sqrt{2}} \bar{e}\gamma_\mu(1-\gamma_5)\nu_e \cdot \bar{\nu}_\mu\gamma^\mu(1-\gamma_5)\mu$$



$$G_F = \frac{g^2}{4\sqrt{2}m_W^2}$$

Wilson coefficient

# Comparing experiments



- How to compare different nuclear beta decays?
  - Effective Lagrangian at the **hadron** level!

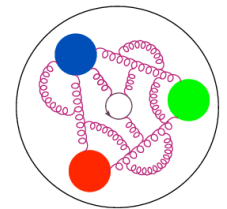
$$\begin{aligned}
 -\mathcal{L}_{n \rightarrow pe-\bar{\nu}_e} = & \bar{p} n (C_S \bar{e} \nu_e - C'_S \bar{e} \gamma_5 \nu_e) \\
 & + \bar{p} \gamma^\mu n (C_V \bar{e} \gamma_\mu \nu_e - C'_V \bar{e} \gamma_\mu \gamma_5 \nu_e) \\
 & + \frac{1}{2} \bar{p} \sigma^{\mu\nu} n (C_T \bar{e} \sigma_{\mu\nu} \nu_e - C'_T \bar{e} \sigma_{\mu\nu} \gamma_5 \nu_e) \\
 & - \bar{p} \gamma^\mu \gamma_5 n (C_A \bar{e} \gamma_\mu \gamma_5 \nu_e - C'_A \bar{e} \gamma_\mu \nu_e) \\
 & + \bar{p} \gamma_5 n (C_P \bar{e} \gamma_5 \nu_e - C'_P \bar{e} \nu_e) + \text{h.c.}
 \end{aligned}$$

[Lee & Yang '1956]

- How to compare with e.g. pion decays?
  - Effective Lagrangian at the **quark** level!

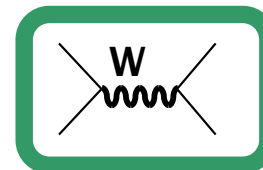
$$\mathcal{L}_{d \rightarrow ul-\bar{\nu}_e} = -\frac{4G_F V_{ij}}{\sqrt{2}} \left[ \bar{\ell}_L \gamma_\mu \nu \cdot \bar{u} \gamma^\mu d_L + \sum_{\rho\delta\Gamma} \epsilon_{\rho\delta}^\Gamma \bar{\ell}_\rho \Gamma \nu \cdot \bar{u} \Gamma d_\delta \right]$$

$$\mathbf{C}_i \sim \mathbf{FF} \times \boldsymbol{\varepsilon}_i$$



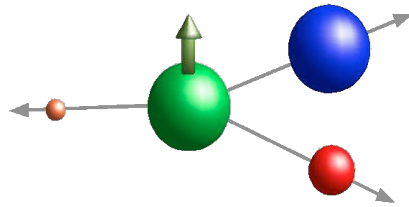
- How to compare with LHC experiments?
  - Effective Lagrangian at the **quark** level at the EW scale!

$$\mathcal{L}_{eff.} = \mathcal{L}_{SM} + \frac{1}{\Lambda^2} \sum \alpha_i \mathcal{O}_i$$



Hadrons:

$$n \rightarrow p e^- \bar{\nu}$$



# Hadronic EFT

[Lee & Yang'1956]

$$\begin{aligned} -\mathcal{L}_{n \rightarrow pe^- \bar{\nu}_e} &= C_V \left( \bar{p} \gamma^\mu n + \frac{C_A}{C_V} \bar{p} \gamma^\mu \gamma_5 n \right) \times \bar{e} \gamma_\mu (1 - \gamma_5) \nu_e \\ &+ C_S \bar{p} n \times \bar{e} (1 - \gamma_5) \nu_e + \frac{1}{2} C_T \bar{p} \sigma^{\mu\nu} n \times \bar{e} \sigma_{\mu\nu} (1 - \gamma_5) \nu_e \\ &- C_P \bar{p} \gamma_5 n \times \bar{e} (1 - \gamma_5) \nu_e + \text{h.c.} \\ &+ \text{terms with RH neutrinos} \end{aligned}$$

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SM terms

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~~← terms with RH neutrinos~~

*Linear approx:*

*SM + small + (small)<sup>2</sup>*

*(Or simply no  $\nu_R$ :  $C_i = C_i'$ )*

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 \end{aligned}$$

~~$C_P \bar{p} \gamma_5 n \times \bar{e} (1 - \gamma_5) \nu_e + \text{h.c.}$~~  →

~~← terms with RH neutrinos~~

“since the nucleons are treated nonrelativistically, the pseudoscalar couplings are omitted”

Linear approx:  
 SM + small + (small)<sup>2</sup>  
 (Or simply no  $\nu_R$ :  $C_i = C_i'$ )

Wrong reason...  $C_P = 348(11) \epsilon_P$   
 [MGA & Camalich, PRL 112 (2014)]

Real reason: the bounds on  $\epsilon_P$  from pion decays are much stronger!!!

$$|\mathcal{A}(\pi \rightarrow l\nu)|^2 \sim m_\ell^2 \left( 1 + \frac{M_{QCD}}{m_\ell} \epsilon_P \right)^2$$

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$G_F V_{ud} (1 + NP)$

[Lifetime shift]

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 \neq 1$$

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$g_A (1 + NP)$

Only way out:  
lattice QCD!

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 & + \underbrace{C_S}_{\downarrow} \bar{p} n \times \bar{e} (1 - \gamma_5) \nu_e + \frac{1}{2} \underbrace{C_T}_{\downarrow} \bar{p} \sigma^{\mu\nu} n \times \bar{e} \sigma_{\mu\nu} (1 - \gamma_5) \nu_e + \text{h.c.}
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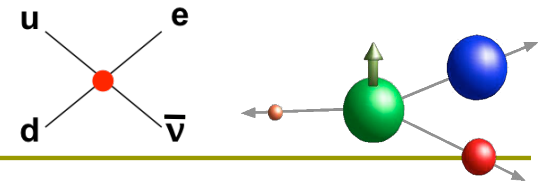
**S and T affect the angular distributions and the spectrum!!**

$$\frac{d\Gamma(\mathbf{J})}{dE_e d\Omega_e d\Omega_\nu} \sim \xi(E) \left\{ 1 + a \frac{\mathbf{p}_e \cdot \mathbf{p}_\nu}{E_e E_\nu} + \underbrace{b \frac{m_e}{E_e}}_{\circlearrowleft} + A \frac{\mathbf{p}_e \cdot \mathbf{J}}{E_e J} + (B + b_B \frac{m_e}{E_e}) \frac{\mathbf{p}_\nu \cdot \mathbf{J}}{E_\nu J} \right\}$$

$$b_{(B)} = \# C_S + \# C_T \quad \text{Fierz term [1937]}$$

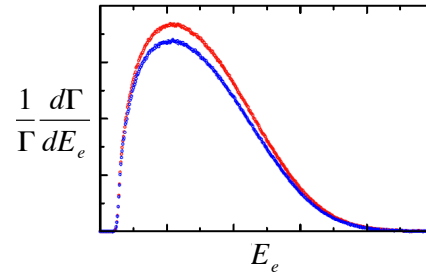
[+ CPV effects]

# Probing the Fierz term

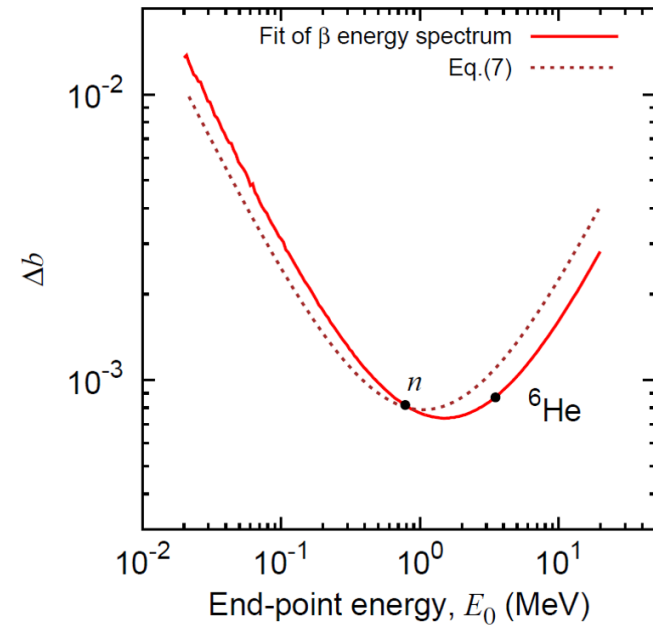


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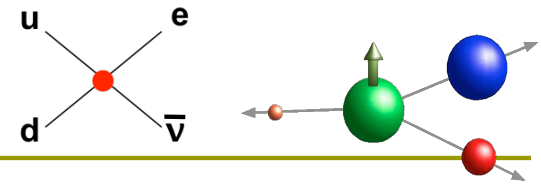
✓ Direct effect in the spectrum:



Optimal endpoint: 1-4 MeV  
[MGA & Naviliat-Cuncic, PRC94 (2016)]

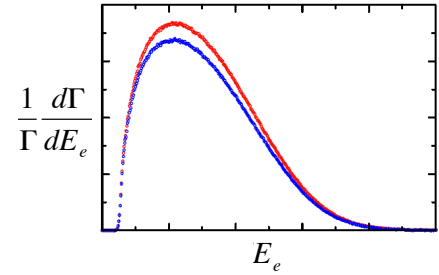


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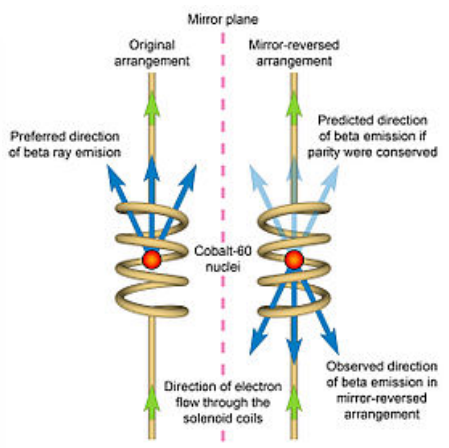


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✓ Indirect effect in the asymmetries:

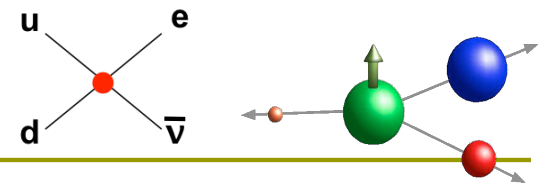
$$\tilde{X} = \frac{X}{1 + b \langle m/E_e \rangle}$$

PS: Not always valid!  
(proton spectrum)  
[MGA & Naviliat-Cuncic, PRC94 (2016)]



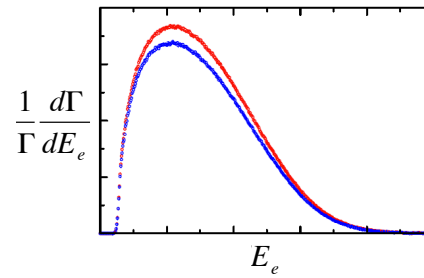


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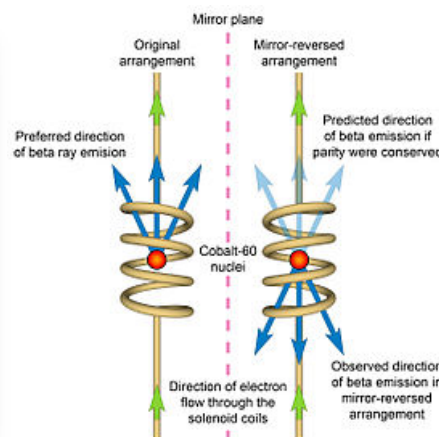


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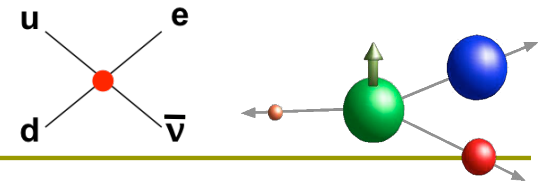
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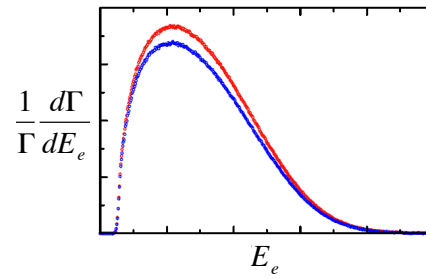
Talks by X. Flechard & R. Combe  
on Thursday about these  
measurements in GANIL & ISOLDE

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[MGA & Naviliat-Cuncic, PRC94 (2016)]

✓ Indirect effect in the asymmetries:

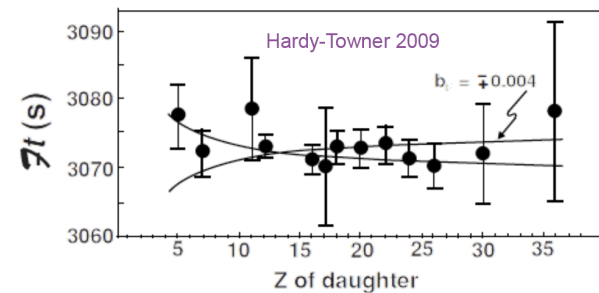
$$\tilde{X} = \frac{X}{1 + b \langle m/E_e \rangle}$$

PS: Not always valid!  
(proton spectrum)  
[MGA & Naviliat-Cuncic, PRC94 (2016)]

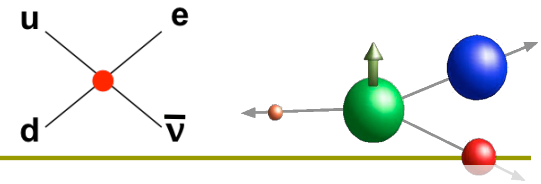
✓ Indirect effect in the Ft-values & neutron lifetime:



$$\delta\tau_n, \delta Ft \sim -b \left\langle \frac{m_e}{E_e} \right\rangle$$



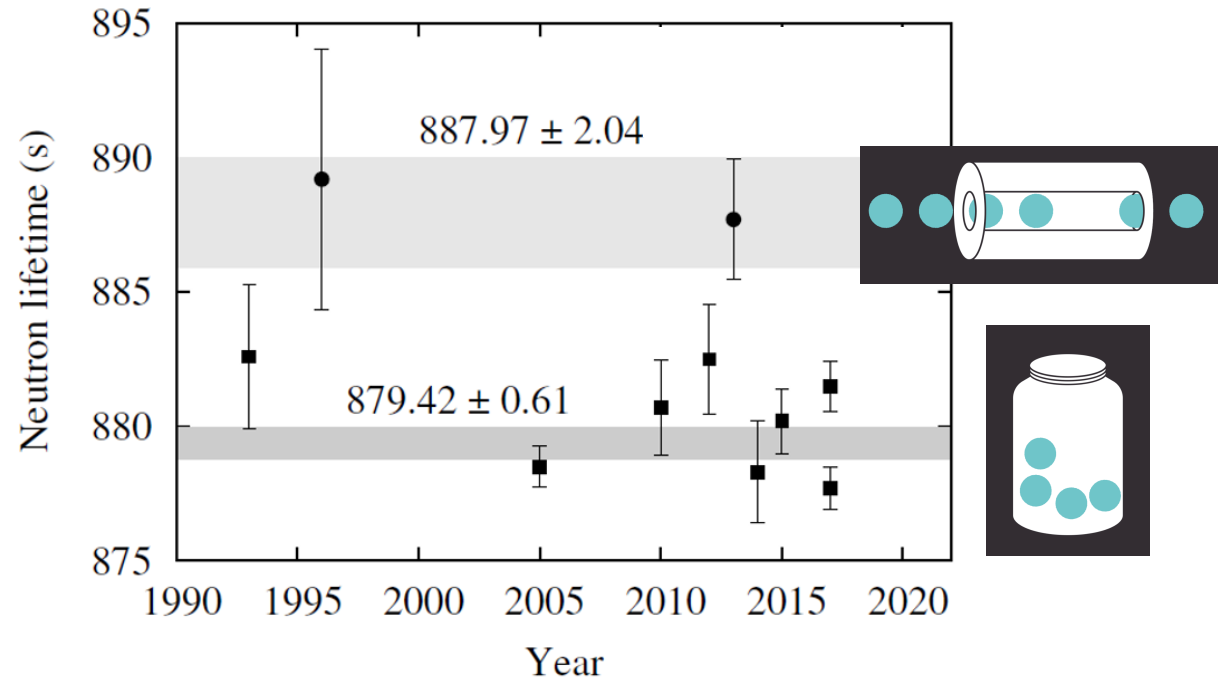
# Probing the Fierz term



Heavy NP cannot explain the beam vs. bottle tension

.... Light NP?

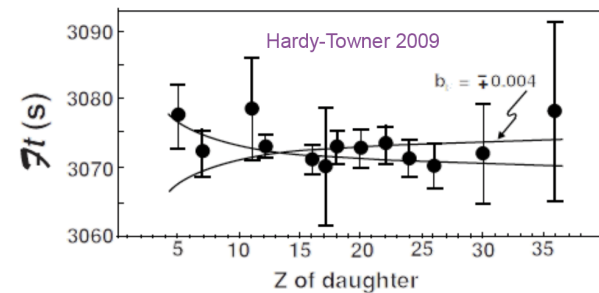
[Fornal & Grinstein PRL (120 (2018))]



✓ Indirect effect in the Ft-values & neutron lifetime:

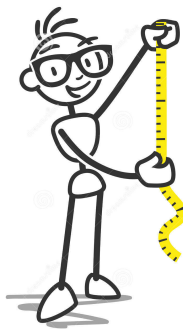


$$\delta\tau_n, \delta Ft \sim -b \left\langle \frac{m_e}{E_e} \right\rangle$$



# Current data

Precision:  
0(0.01 - 1)% !!



[MGA, O. Naviliat Cuncic, N. Severijns, Prog. Part. Nucl. Phys. 104 (2019) 165-223]

## Nuclei

### $Ft(0^+ \rightarrow 0^+)$ values

Parent	$Ft$ (s)
$^{10}\text{C}$	$3078.0 \pm 4.5$
$^{14}\text{O}$	$3071.4 \pm 3.2$
$^{22}\text{Mg}$	$3077.9 \pm 7.3$
$^{26m}\text{Al}$	$3072.9 \pm 1.0$
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$^{54}\text{Co}$	$3069.8 \pm 2.6$
$^{62}\text{Ga}$	$3071.5 \pm 6.7$
$^{74}\text{Rb}$	$3076.0 \pm 11.0$

[Hardy-Towner'2015]

### Correlation coefficients

Parent	Type	Parameter	Value
$^6\text{He}$	GT/ $\beta^-$	$a$	$-0.3308(30)^a$
$^{32}\text{Ar}$	F/ $\beta^+$	$\tilde{a}$	0.9989(65)
$^{38m}\text{K}$	F/ $\beta^+$	$\tilde{a}$	0.9981(48)
$^{60}\text{Co}$	GT/ $\beta^-$	$\tilde{A}$	$-1.014(20)$
$^{67}\text{Cu}$	GT/ $\beta^-$	$\tilde{A}$	0.587(14)
$^{114}\text{In}$	GT/ $\beta^-$	$\tilde{A}$	$-0.994(14)$
$^{14}\text{O}/^{10}\text{C}$	F-GT/ $\beta^+$	$P_F/P_{GT}$	0.9996(37)
$^{26}\text{Al}/^{30}\text{P}$	F-GT/ $\beta^+$	$P_F/P_{GT}$	1.0030 (40)
$^8\text{Li}$	GT/ $\beta^-$	$R$	0.0009(22)

### Neutron data

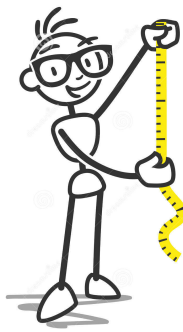
Parameter	Value
$\tau_n$ (s)	879.75(76) * ( $S = 1.9!!$ )
$a_n$	$-0.1034(37)$ *
$\tilde{a}_n$	$-0.1090(41)$
$\tilde{A}_n$	$-0.11869(99)$ * ( $S = 2.6!!$ )
$\tilde{B}_n$	0.9805(30) *
$\lambda_{AB}$	$-1.2686(47)$
$D_n$	$-0.00012(20)$ *
$R_n$	0.004(13)

\* Average

$$S = (\chi^2_{\min}/\text{dof})^{1/2}$$

# Current data (+ TH!!)

Precision:  
0(0.01 - 1)% !!



[MGA, O. Naviliat Cuncic, N. Severijns, Prog. Part. Nucl. Phys. 104 (2019) 165-223]

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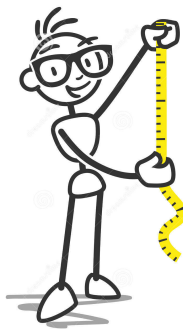
[Hardy-Towner'2015]

Th: QED + Isospin symmetry breaking corrections

$$Ft_i \equiv ft_i (1 + \delta'_R) (1 + \delta_{NS} - \delta_C)$$

# Current data (+ TH!!)

Precision:  
0(0.01 - 1)% !!



[MGA, O. Naviliat Cuncic, N. Severijns, Prog. Part. Nucl. Phys. 104 (2019) 165-223]

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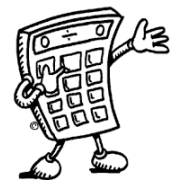
$$Ft_i \equiv ft_i (1 + \delta'_R) (1 + \delta_{NS} - \delta_C)$$

**NEW** Including Perkeo-III, PRL122 (2019):  
 $a_n = -0.11958(18)$  [ $S=1$ ]  $\rightarrow$  5x!

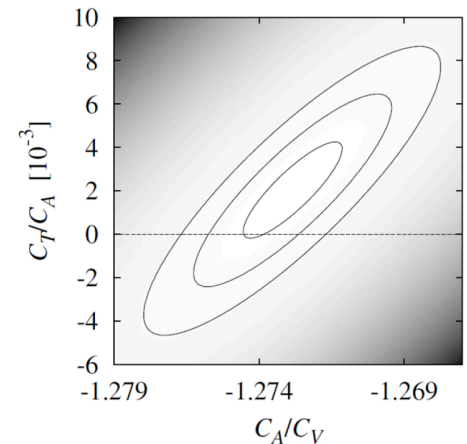
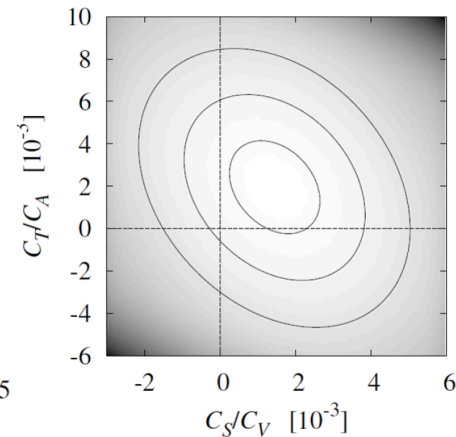
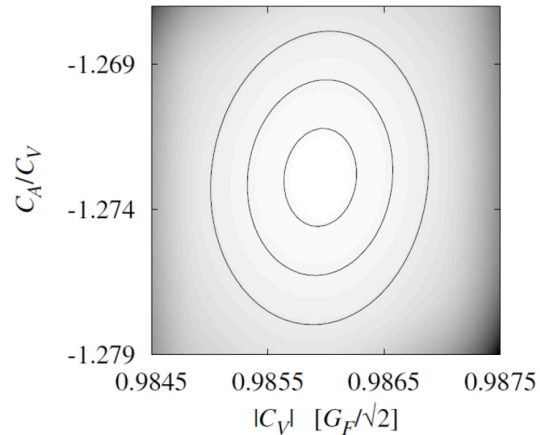
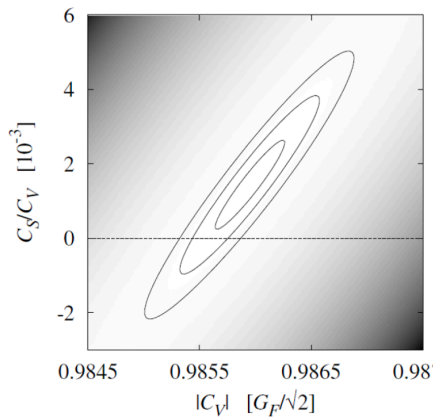
**NEW** Including aSPECT (1908.04785):  
 $a_n = -0.10426(82)$   $\rightarrow$  6x!

**NEW** Nuclear structure-dep. corrections?  
[Seng, Gorchtein, & Ramsey-Musolf, PRD100 (2019)]  
[Gorchtein, PRL123 (2019)]

# Current data → Results



$$\begin{pmatrix} |C_V| \\ C_A/C_V \\ C_S/C_V \\ C_T/C_A \end{pmatrix} = \begin{pmatrix} 0.98595(34) G_F/\sqrt{2} \\ -1.2728(17) \\ 0.0014(12) \\ 0.0020(22) \end{pmatrix} \quad \text{with} \quad \rho = \begin{pmatrix} 1.00 & & & \\ 0.08 & 1.00 & & \\ 0.94 & 0.08 & 1.00 & \\ -0.32 & 0.85 & -0.31 & 1.00 \end{pmatrix}$$

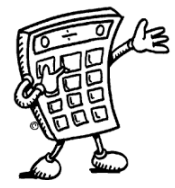


Driven by  
Ft's,  $T_n$ ,  $A_n$ !

[MGA, O. Naviliat Cuncic, N. Severijns,  
Prog. Part. Nucl. Phys. 104 (2019)]



# Current data $\rightarrow$ Results



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- One can trivially calculate the precision needed in any other observable to compete:

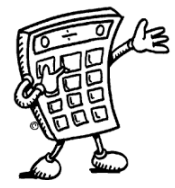
Example:

$$b_{GT} = f(C_i) \rightarrow \delta b_{GT} = 0.004$$

Reachable! (NSCL, UW-Seattle?, GANIL?)!



# Current data → Results



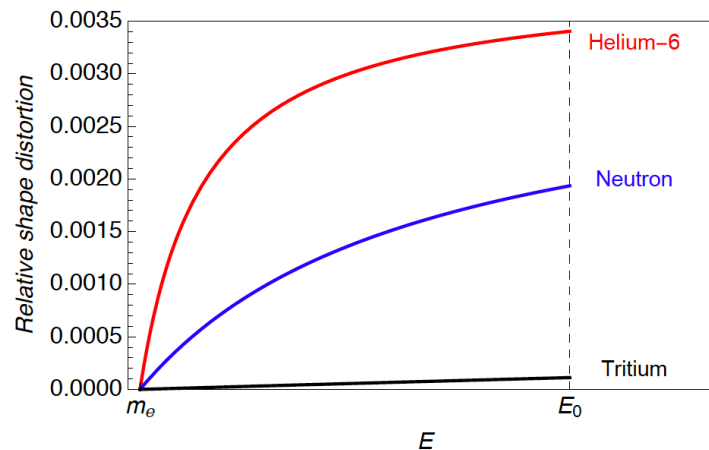
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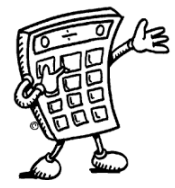
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Reachable! (NSCL, UW-Seattle?, GANIL?)!

## Spectrum shape measurements



# Current data $\rightarrow$ Results

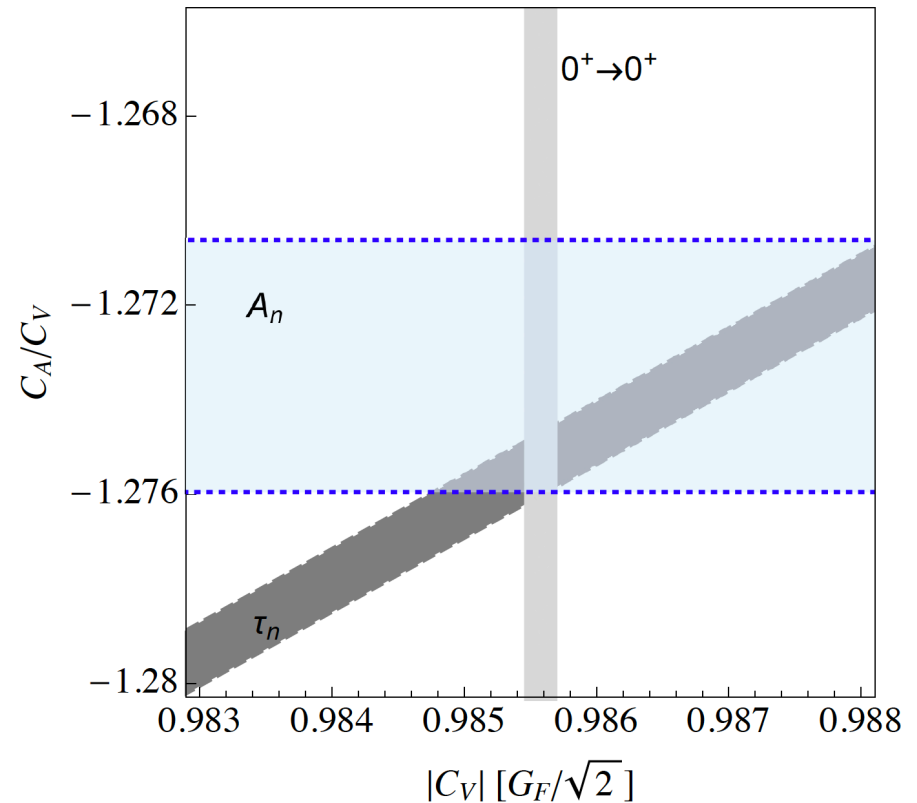


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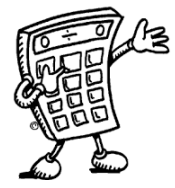
SM Limit



$$\begin{aligned} |C_V| &= 0.98559(11) G_F/\sqrt{2} \\ C_A/C_V &= -1.27510(66), \\ &(\rho = 0.25) \end{aligned}$$



# Current data $\rightarrow$ Results

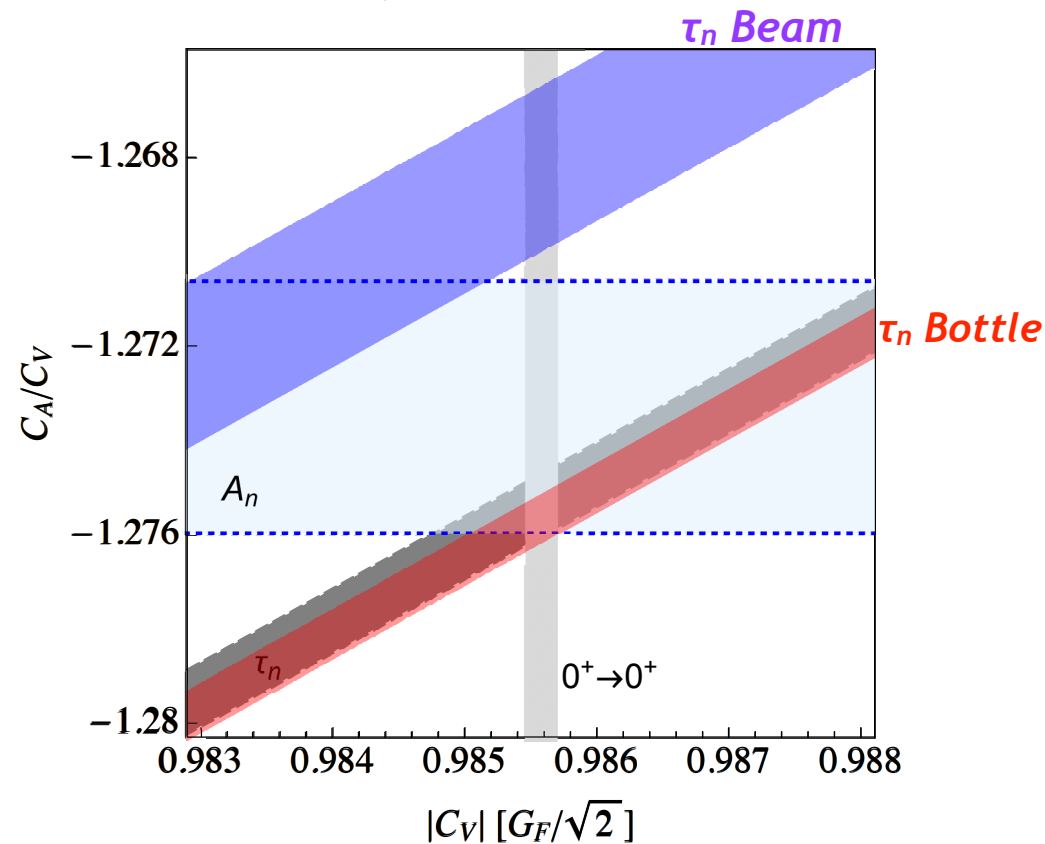


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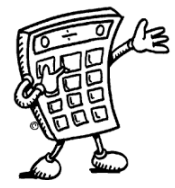
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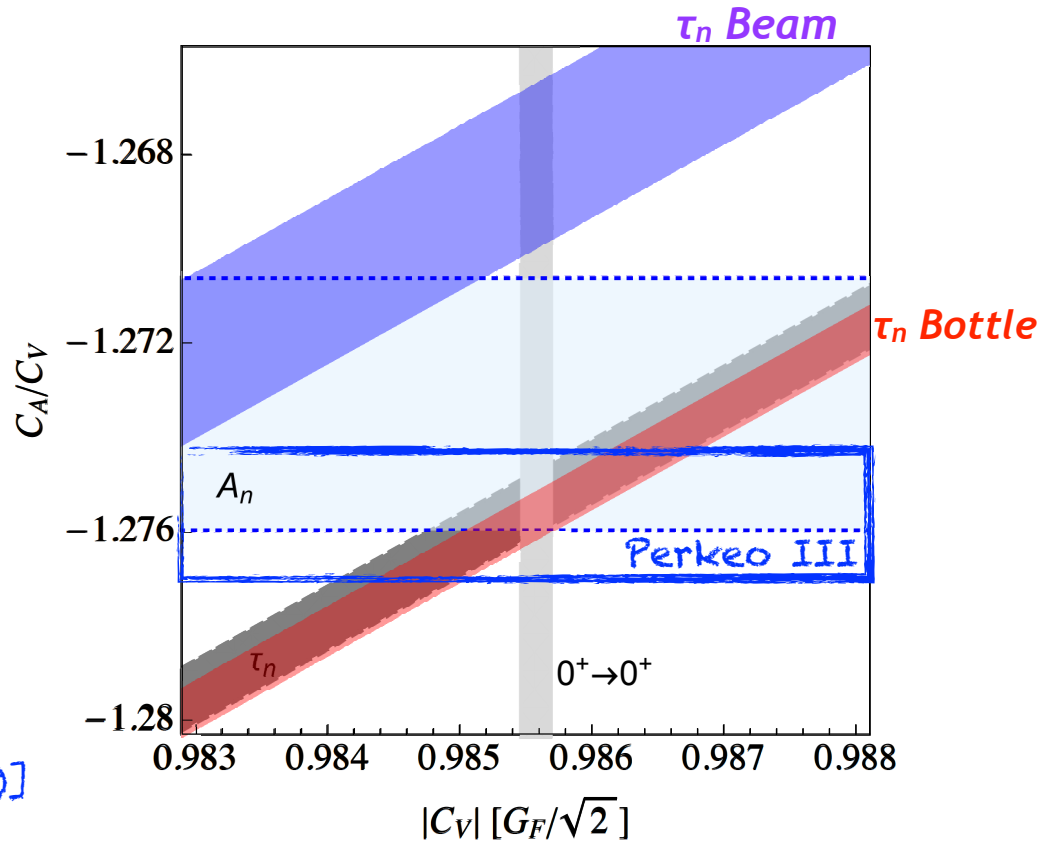


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**NEW**

$A_n = -0.11983(21)$  [Perkeo III, 2.5x!]  
 → no dark channel  
 [Dubbers et al, PLB791 (2019);  
 Czarnecki-Marciano-Sirlin, PRL120 (2018)]

# Interlude I: mirror beta decays?

- $\beta$  transitions between isobaric analog states in  $T = 1/2$  isospin doublets;  
→  $|M_F|^2 = 1$  and nonzero F/GT mixing ratio (neutron!).

- Many per-mil level determinations of the  $Ft$  values! (Exp + Th)

[Severijns et al, PRC78 (2008); Hayen & Severijns, 1906.09870; etc.]

- But mixing ratios are unknown

→ another observable (asymmetries!) needed;

$^A_j\text{Decay}$	$\mathcal{F}t$ [sec]	asymmetry
$^{19}_{1/2}\text{Ne} \rightarrow \text{F}$	1721.44(92) [10]	$A_{\beta,0} = -0.0391(14)$
$^{21}_{3/2}\text{Na} \rightarrow \text{Ne}$	4071(4) [11]	$\tilde{a}_{\beta\nu} = 0.5502(60)$
$^{35}_{3/2}\text{Ar} \rightarrow \text{Cl}$	5688.6(7.2)	$\tilde{A}_{\beta} = 0.430(22)$
$^{37}_{3/2}\text{K} \rightarrow \text{Ar}$	4605.4(8.2) [12]	$\tilde{A}_{\beta} = -0.5707(19)$ [13]

NOTE: LPCTrap analysis  
ongoing for Ne-19 & Ar-35

- SM analysis: [Naviliat-Cuncic & Severijns, PRL102 (2009)]

$V_{ud}$  can be extracted with 0.1% precision!

Although (*currently!*) not competitive, it's a nontrivial crosscheck;

- What about BSM? [Falkowski, MGA & Naviliat-Cuncic, work in progress]

- In the absence of RH neutrinos, the situation is much like in the SM;
- Once RH neutrinos are introduced that's not the case.

# Interlude II: CP violation?

- If the EFT coefficients are complex, CP-violating effects appear;
- CP violation of "standard" origin is way too small in  $\beta$  decays;
- Beta decay data (D & R correlations)  $\rightarrow$   $\text{Im}(C_A/C_V) = -0.00034(59)$ ,  
 $\text{Im}(C_S/C_V) = -0.007(30)$ ,  
 $\text{Im}(C_T/C_A) = 0.0004(33)$ ,  
[MGA, O. Naviliat Cuncic, N. Severijns,  
Prog. Part. Nucl. Phys. 104 (2019) 165-223]
- Improvements also expected:

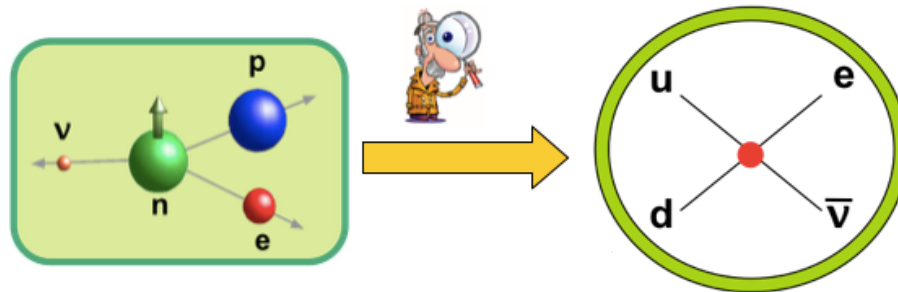
Coefficient	Precision goal	Experiment (Laboratory)	Comments
D	$\mathcal{O}(10^{-4})$ [418]	MORA (GANIL/JYFL) [418]	In preparation ( $^{23}\text{Mg}$ )
R	$\mathcal{O}(10^{-3})$ [427]	MTV (TRIUMF) [427-429]	Data taking ongoing ( $^8\text{Li}$ )
D, R	$\mathcal{O}(0.1)\%$ [399]	BRAND (ILL) [399,400]	Proposal

ANR funded!

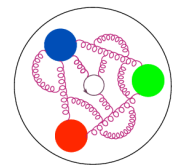
[ E. Liénard's talk, Thu 11:10 ]

Quarks (low-E):

$$d \rightarrow u e^- \bar{\nu}$$



# From hadrons to quarks



$$\begin{aligned}C_V &\sim g_V G_F^\mu V_{ud} (1 + \text{NP}) (1 + \text{RC}) \\C_A/C_V &\sim -g_A/g_V (1 - 2\epsilon_R) \\C_S &\sim g_S \epsilon_S \\C_T &\sim g_T \epsilon_T\end{aligned}$$

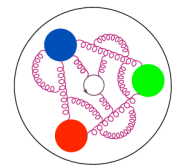
[Lifetime shift]

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 \neq 1$$

$$\tilde{V}_{ud} \equiv V_{ud} (1 + \epsilon_L + \epsilon_R) \left(1 - \frac{\delta G_F}{G_F}\right)$$



# From hadrons to quarks

 $\tilde{V}_{ud}$ 

$$C_V \sim g_V G_F^\mu \tilde{V}_{ud} (1 + \text{NP}) (1 + \text{RC})$$

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$$C_S \sim g_S \epsilon_S$$

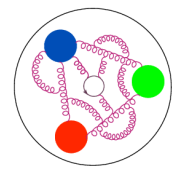
$$C_T \sim g_T \epsilon_T$$

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$$C_T \sim g_T \epsilon_T$$

[Lifetime shift]

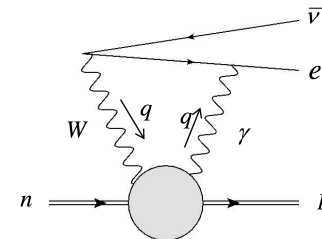
$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 \neq 1$$

Inner RC:

2.361(38)% [Marciano-Sirlin, PRL96 (2006)]

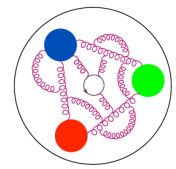
2.467(22)% [Seng et al., PRL121 (2018)]

2.426(32)% [Czarnecki et al., 1907.06737]



$$\tilde{V}_{ud} \equiv V_{ud} (1 + \epsilon_L + \epsilon_R) \left( 1 - \frac{\delta G_F}{G_F} \right)$$

# From hadrons to quarks

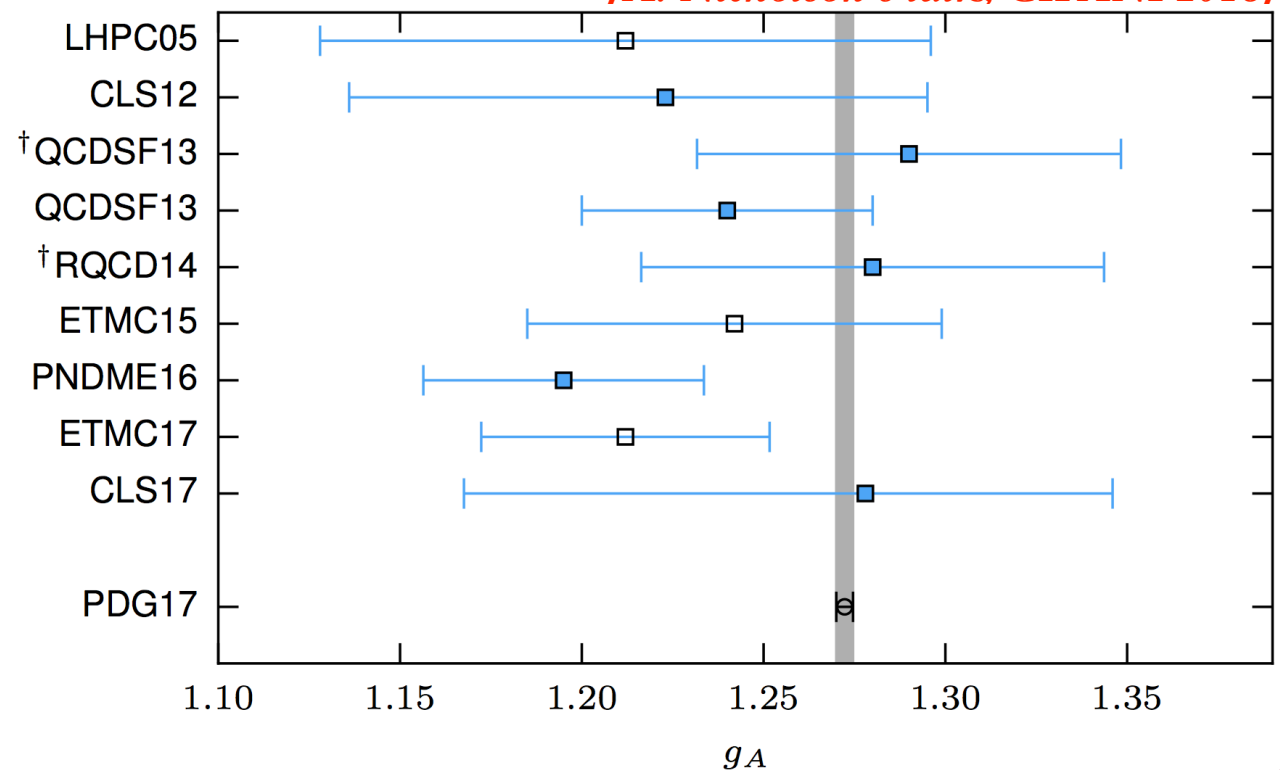


$$\begin{aligned}
 C_V &\sim g_V G_F^\mu V_{ud} (1 + \text{NP}) (1 + \text{RC}) \\
 C_A/C_V &\sim -g_A/g_V (1 - 2\epsilon_R) \\
 C_S &\sim g_S \epsilon_S \\
 C_T &\sim g_T \epsilon_T
 \end{aligned}$$

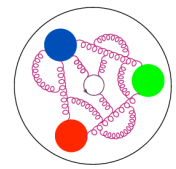
*Axial charge*

$$g_A \rightarrow \langle p | \bar{u} \gamma_\mu \gamma_5 d | n \rangle$$

*[A. Nicholson's talk, CIPANP2018]*



# From hadrons to quarks



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$$g_A \rightarrow \langle p | \bar{u} \gamma_\mu \gamma_5 d | n \rangle$$

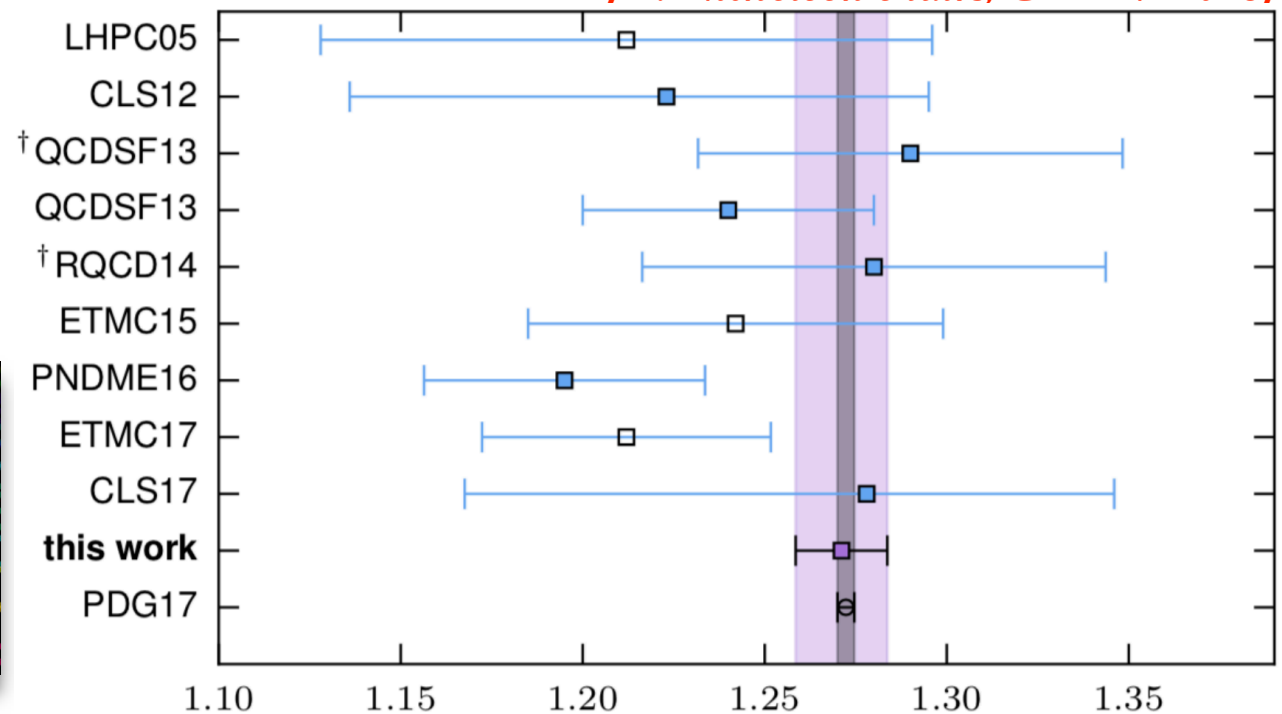


$$g_A^{\text{LQCD}} = 1.271 \pm 0.013$$

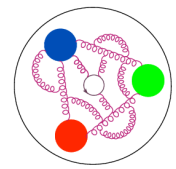
*Nature*, May 30, 2018

C.C. Chang, A.N., E. Rinaldi, E. Berkowitz, N. Garron, D. Brantley, H. Monge-Camacho, C. Monahan, C. Bouchard, M.A. Clark, B. Joo, T. Kurth, K. Orginos, P. Vranas, A. Walker-Loud

*[A. Nicholson's talk, CIPANP2018]*



# From hadrons to quarks



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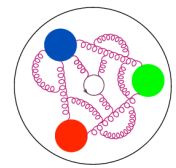
BUT...

- PNDME'18:  $g_A = 1.218(39)$

"We argue that our error estimate is more realistic"

- FLAG average:  $g_A = 1.251(33)$

# From hadrons to quarks



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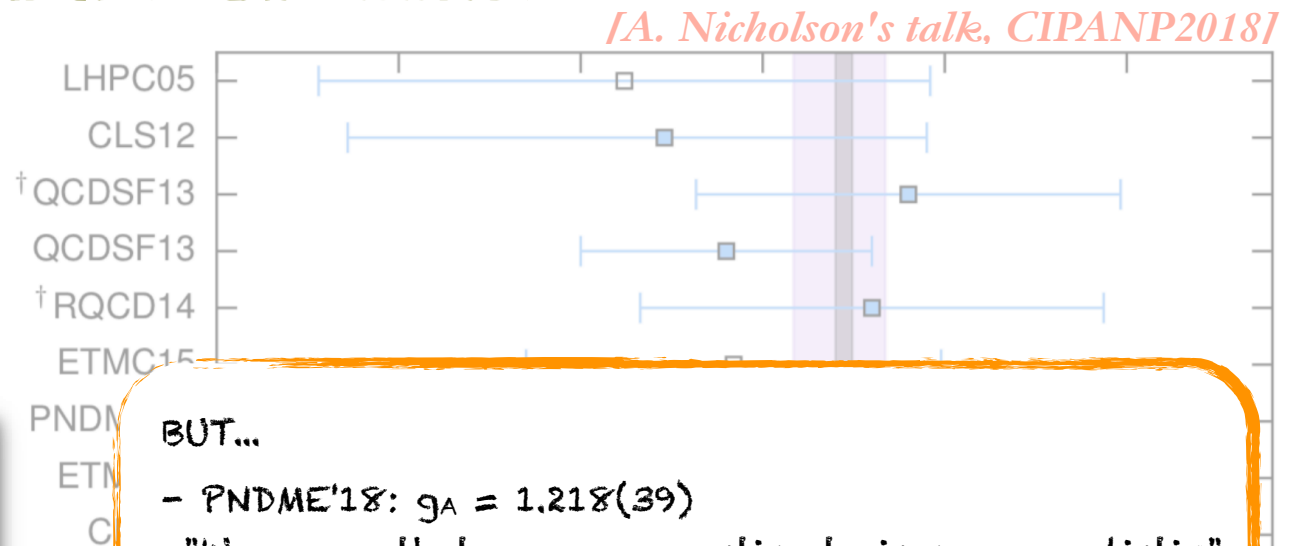
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*Nature*, May 30, 2018

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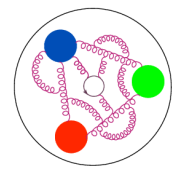
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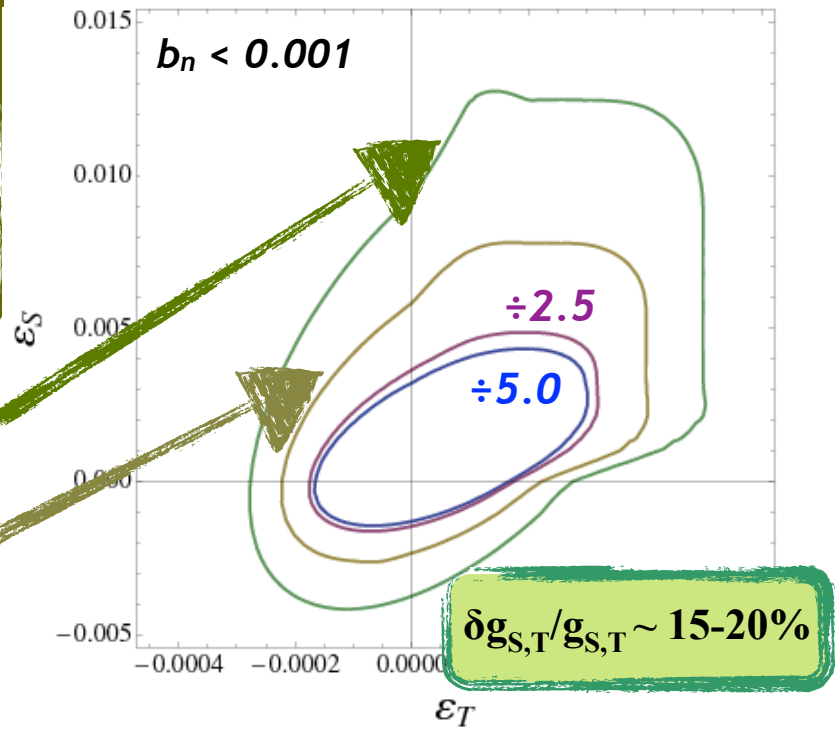
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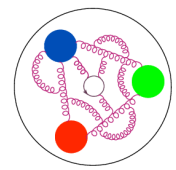
*Scalar & tensor charges*

	$\langle p \bar{u}d n\rangle$	$\langle p \bar{u}\sigma_{\mu\nu}\gamma_5 d n\rangle$
	$g_S$	$g_T$
<i>Adler et al. '1975 (quark model)</i>	0.60(40)	1.45(85)
<i>PNDME 2011</i>	0.80(40)	1.05(35) <i>[average]</i>



[Bhattacharya, Cirigliano, Cohen, Filipuzzi, MGA, Graesser, Gupta, Lin, PRD85 (2012)]

# From hadrons to quarks



$$C_V \sim g_V G_F^\mu V_{ud} (1 + \text{NP}) (1 + \text{RC})$$

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	$g_S$	$g_T$
Adler et al. '1975 (quark model)	0.60(40)	1.45(85)
PNDME 2011	0.80(40)	1.05(35)
LHPC 2012	1.08(32)	1.04(02)
RQCD 2014	1.02(35)	1.01(02)
PNDME 2013/15	0.72(32)	1.02(08)
ETMC 2015/17	0.93(33)	1.00(03)
CVC	1.02(11)	-
PNDME 2016/18	1.02(10)	0.99(03)
JLQCD'18	0.88(11)	1.08(10)
...	...	...

*All syst!*

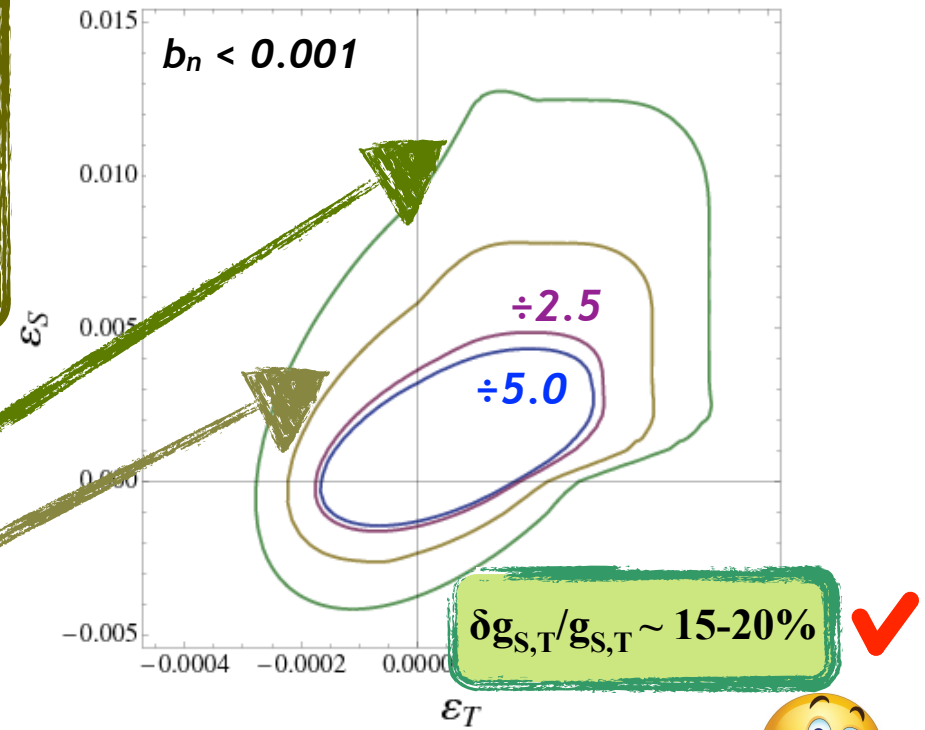
[Bhattacharya et al.,  
Phys. Rev. Lett. 115 (2015)]

$$g_S = \frac{(M_n - M_p)_{\text{QCD}}}{m_d - m_u} g_V$$

[MGA & Camalich,  
Phys. Rev. Lett. 112 (2014)]

$g_S = 1.00(8)$

using  $(m_d - m_u)$  from 1802.04248





# From hadrons to quarks

[MGA, O. Naviliat Cuncic, N. Severijns,  
Prog. Part. Nucl. Phys. 104 (2019)]

Using these RC + charges, the  $C_i$  bounds translate into...

BSM fit

$$\begin{pmatrix} |\tilde{V}_{ud}| \\ \epsilon_R \\ \epsilon_S \\ \epsilon_T \end{pmatrix} = \begin{pmatrix} 0.97452(34)(19) \\ 0.002(1)(21)_{g_A} \quad (90\% \text{ CL}) \\ 0.0014(20)(3)_{g_S} \quad (90\% \text{ CL}) \\ -0.0007(12)(1)_{g_T} \quad (90\% \text{ CL}) \end{pmatrix} \quad \text{with} \quad \rho = \begin{pmatrix} 1.00 & & & \\ 0.00 & 1.00 & & \\ 0.83 & 0.00 & 1.00 & \\ 0.28 & -0.04 & 0.31 & 1.00 \end{pmatrix}$$

# From hadrons to quarks

[MGA, O. Naviliat Cuncic, N. Severijns,  
Prog. Part. Nucl. Phys. 104 (2019)]

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SM fit

$$\begin{aligned} |V_{ud}| &= 0.97416(11)(19)_{RC} = 0.97416(21) , \\ \lambda &= 1.27510(66) , \\ (\rho &= -0.13) \end{aligned}$$

# From hadrons to quarks

[MGA, O. Naviliat Cuncic, N. Severijns, Prog. Part. Nucl. Phys. 104 (2019)]

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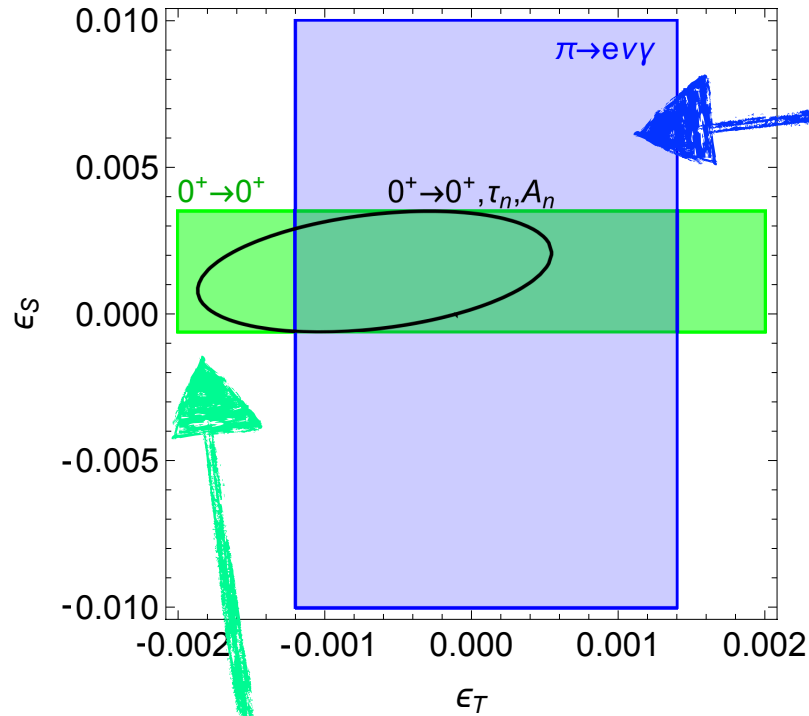
- 0.97370(14) Seng et al. PRL121 (2018)
- 0.97389(22) Seng et al. PRD100 (2019)
- 0.97365(28) Gorchtein, PRL123 (2019)
- 0.97389(18) Czarnecki et al. 1907.06737

**NEW**

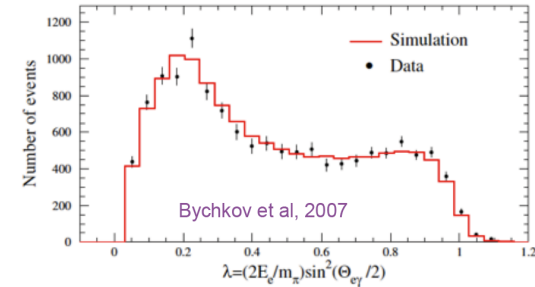


# From hadrons to quarks

[MGA, O. Naviliat Cuncic, N. Severijns, Prog. Part. Nucl. Phys. 104 (2019)]



$\pi \rightarrow e\nu\gamma$   
(PIBETA '2009)



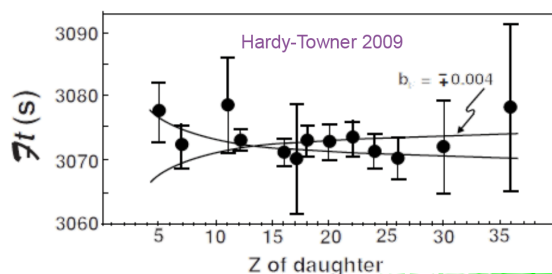
$$\langle \gamma(\epsilon, p) | \bar{u} \sigma_{\mu\nu} \gamma_5 d | \pi^+ \rangle = -\frac{e}{2} f_T (p_\mu \epsilon_\nu - p_\nu \epsilon_\mu),$$

$$f_T = 0.24(4) \quad [\text{Mateu \& Portolés, 2007}]$$

[large-N inspired resonance saturation model]

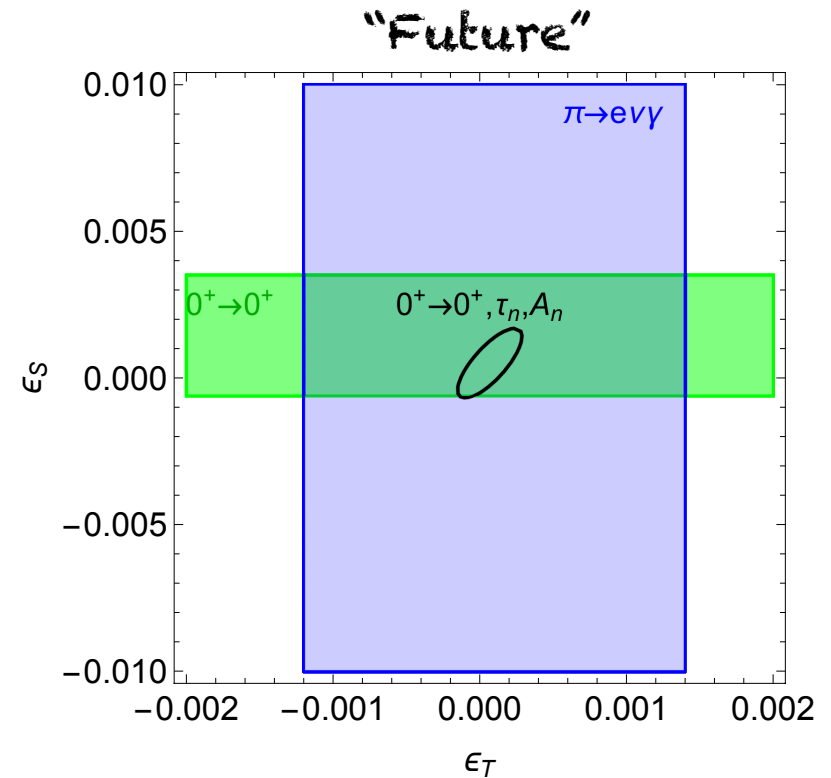
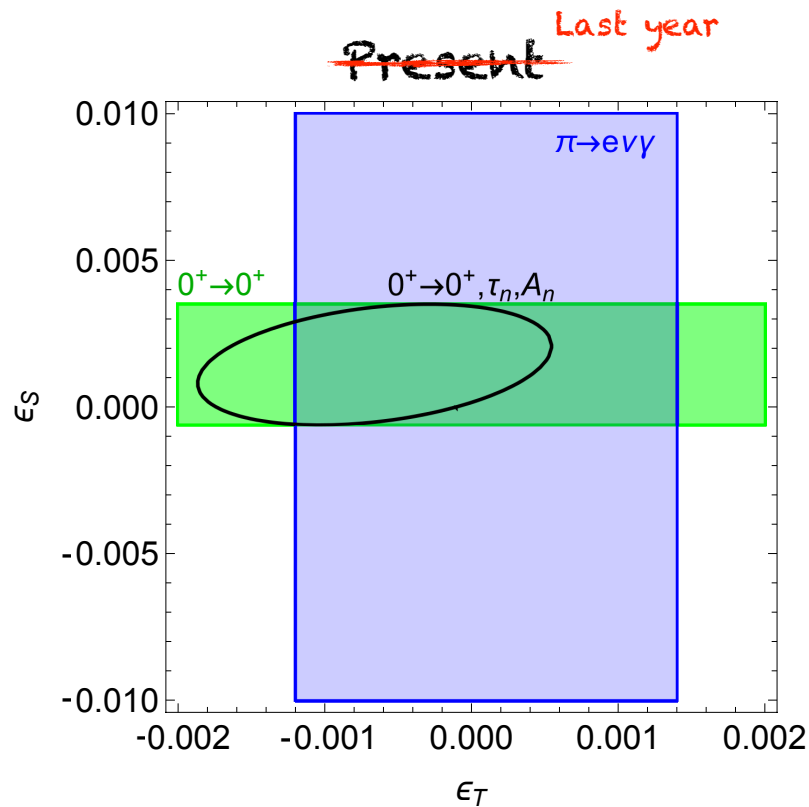
**No LQCD calculation!**

Superaligned nuclear  $\beta$  decays



# From hadrons to quarks

[MGA, O. Naviliat Cuncic, N. Severijns, Prog. Part. Nucl. Phys. 104 (2019)]



**Benchmark numbers**  
(from ongoing / planned experiments):

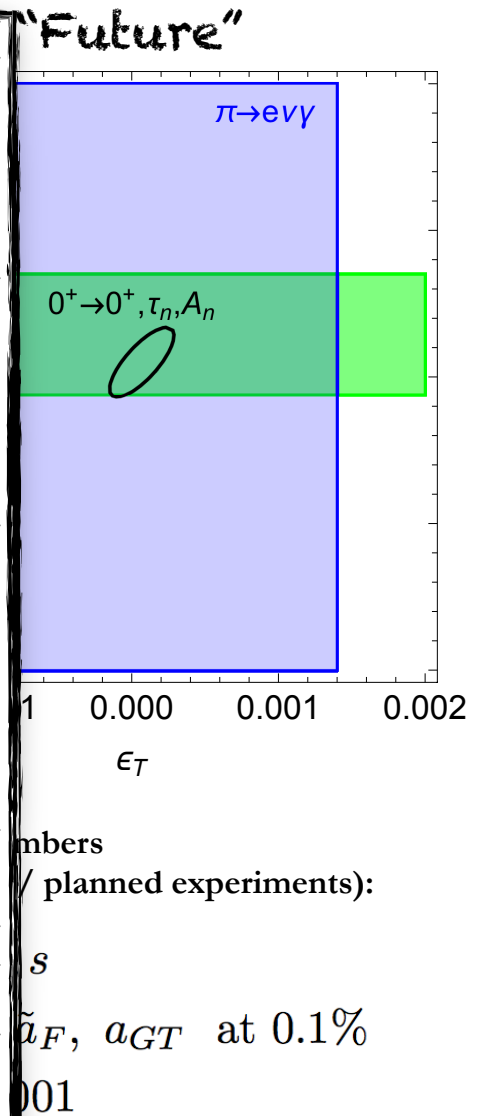
$$\delta\tau_n = 0.1 \text{ s}$$

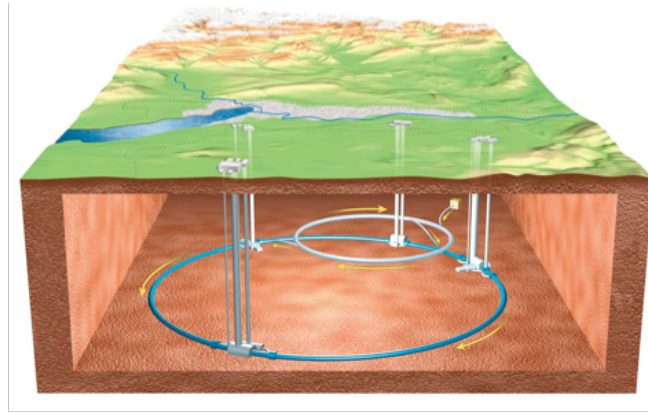
$$\tilde{A}_n, a_n, \tilde{a}_F, a_{GT} \text{ at } 0.1\%$$

$$b_{GT} = 0.001$$

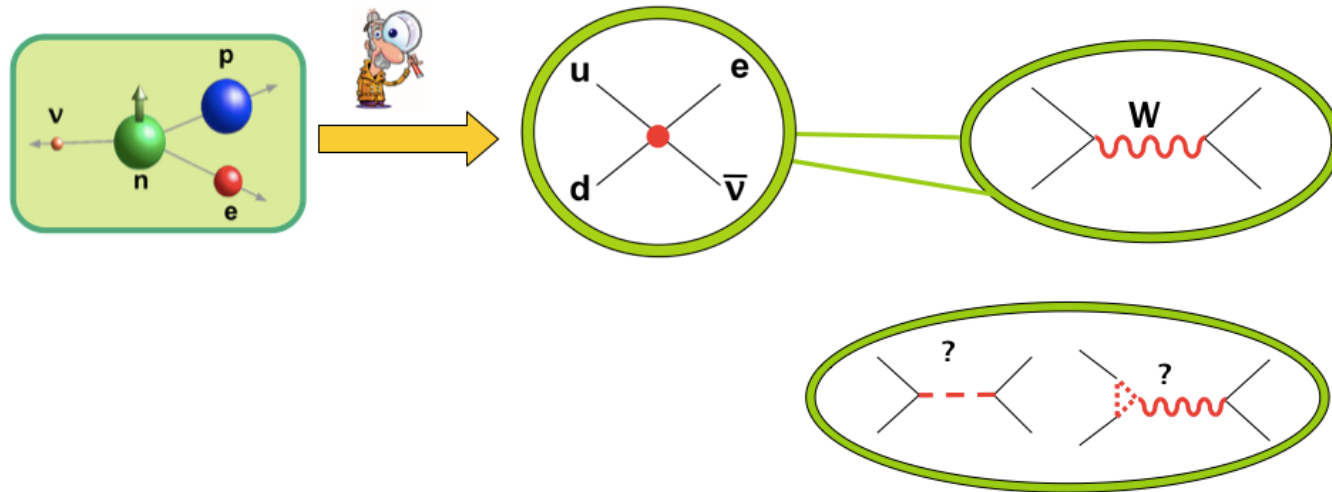
# From hadrons to quarks

Coefficient	Precision goal	Experiment (Laboratory)	Comments
$\tau_n$	1.0 s; 0.1 s [210] 1.0 s; 0.3 s [214] 0.2 s [215] 0.3 s [201] 0.1 s [222] $\leq 0.1$ s [223] 0.5 s [225] 1.0 s; 0.2 s [188]	BL2, BL3 (NIST) [210] LiNA (J-PARC) [211,214] Gravitrapp (ILL) [203,215] Ezhov (ILL) [201] PENeLOPE (Munich) [222] UCN $\tau$ (LANL) [188,189,223,224] HOPE (ILL) [188,225,226] $\tau$ SPECT (Mainz) [188,227]	In preparation; two phases In preparation; two phases Apparatus being upgraded Under construction Being developed Ongoing Proof of principle Ref. [226] Taking data; two phases
$\beta$ -spectrum	$\mathcal{O}(0.01)$ [256]	Supercond. spectr. (Madison) [256]	Shape factor Eq. (51). Ongoing
$\beta$ -spectrum	$\mathcal{O}(0.01)$ [253]	Si-det. spectr. (Saclay) [253,254]	Shape factor Eq. (51). Ongoing
$b_{GT}$	0.001 $\mathcal{O}(0.001)$ [270]	Calorimetry (NSCL) [115,260] miniBETA (Krakow-Leuven) [263-265,270]	Analysis ongoing ( ${}^6\text{He}, {}^{20}\text{F}$ ) Being commissioned
$b_n$	$\mathcal{O}(0.001)$ [276] <0.05 [293,294] 0.03 [295] 0.003 [289] 0.001 [291]	UCNA-Nab-Leuven (LANL) [271,272,276] UCNA (LANL) [390] PERKEO III (ILL) [295] Nab (LANL) [188,289,357,358] PERC (Munich) [291,292]	Analysis ongoing ( ${}^{45}\text{Ca}$ ) Ongoing with $A_n$ data Possible with $A_n$ data In preparation Planned
$a_F$	0.1% [306] 0.1% [343]	TRINAT (TRIUMF) [306,310] TAMUTRAP (TA&M) [343]	Planned ( ${}^{38}\text{K}$ ) Superallowed $\beta p$ emitters
$a$	0.1% [79]	WISArD (ISOLDE) [79,177]	In preparation ( ${}^{32}\text{Ar}$ $\beta p$ decay)
$a_{GT}$	not stated $\mathcal{O}(0.1)\%$ [315] not stated	Ne-MOT (SARAF) [311,312] ${}^6\text{He}$ -MOT (Seattle) [313,315] EIBT (Weizmann Inst.) [316-318]	In preparation ( ${}^{18}\text{Ne}, {}^{19}\text{Ne}, {}^{23}\text{Ne}$ ) Ongoing ( ${}^6\text{He}$ ) In preparation ( ${}^6\text{He}$ )
$a_{mirror}$	0.5% [182]	LPCTrap (GANIL) [182,321,323,324]	Analysis ongoing ( ${}^6\text{He}, {}^{35}\text{Ar}$ )
$\bar{a}_n$	0.5% [273]	NSL-Trap (Notre Dame) [273,344,345]	Planned ( ${}^{11}\text{C}, {}^{13}\text{N}, {}^{15}\text{O}, {}^{17}\text{F}$ )
$a_n$	1.0% [350] 1.0 – 1.5% [351] 0.15% [188,358]	$\alpha$ CORN (NIST) [350,352-354] $\alpha$ SPECT (ILL) [228,229,351] Nab (LANL) [188,289,357,358]	Data taking ongoing Analysis being finalized In preparation
$\bar{A}_n$	0.14% [391] 0.18% [295]	UCNA (LANL) [390] PERKEO III (ILL) [295]	Data taking planned Analysis ongoing
$\bar{A}_{mirror}$	$\mathcal{O}(0.1)\%$ [78]	TRINAT (TRIUMF) [78]	Planned
$\bar{B}_n$	0.01% [397]	UCNB (LANL) [397]	Planned
$\bar{A}_n(a_n, \bar{B}_n, \dots)$	0.05% [291]	PERC (Munich) [291,292]	In preparation
$\bar{A}_n(a_n, \bar{B}_n, \dots)$	< $\mathcal{O}(0.1)\%$ [399]	BRAND (ILL/ESS) [399,400]	Proposed
$D$	$\mathcal{O}(10^{-4})$ [418]	MORA (GANIL/JYFL) [418]	In preparation ( ${}^{23}\text{Mg}$ )
$R$	$\mathcal{O}(10^{-3})$ [427]	MTV (TRIUMF) [427-429]	Data taking ongoing ( ${}^8\text{Li}$ )
$D, R$	$\mathcal{O}(0.1)\%$ [399]	BRAND (ILL) [399,400]	Proposal



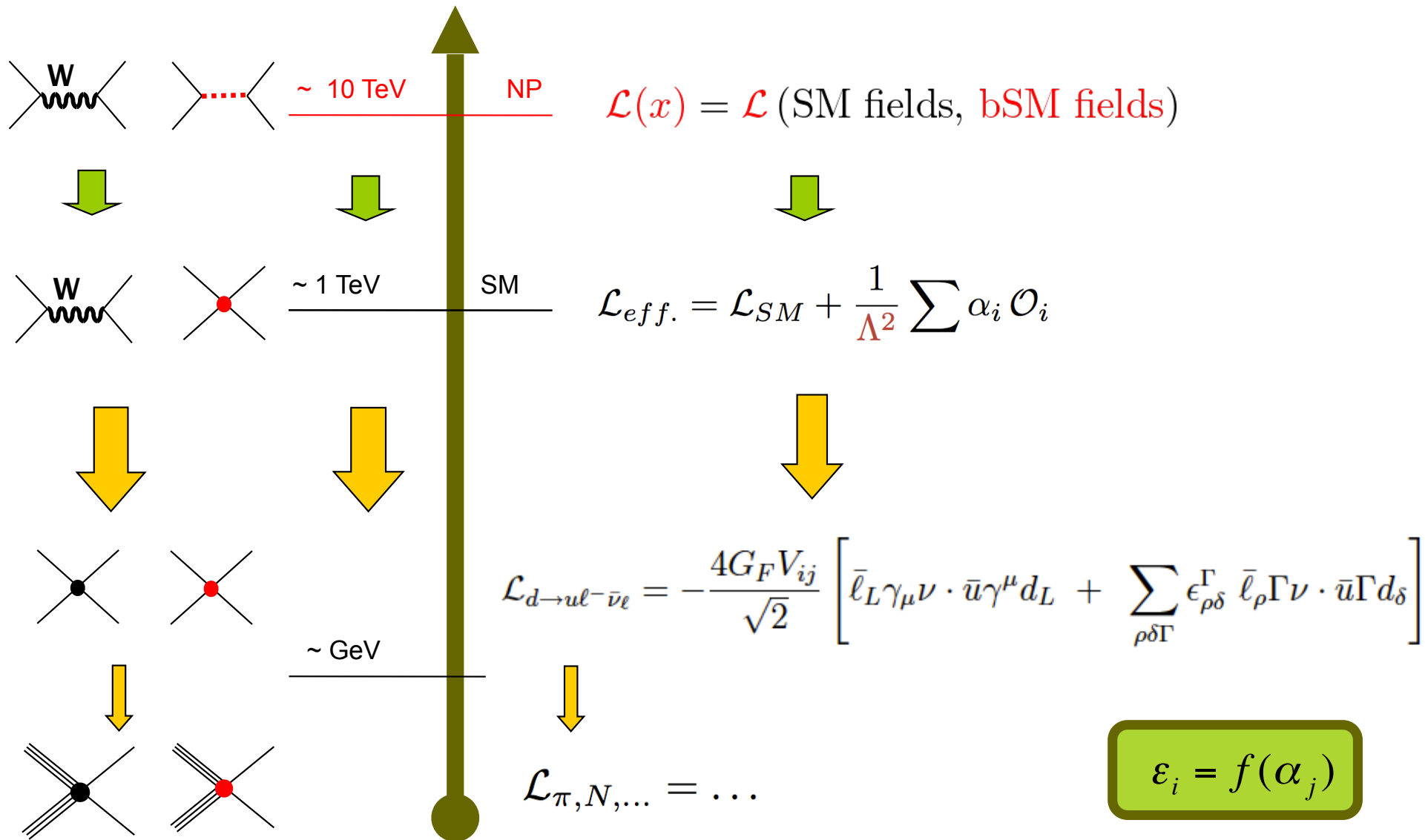


# Quarks, W, Z, ...



# Matching with high-E EFT

$$\frac{d\vec{\epsilon}(\mu)}{d\log\mu} = \left( \frac{\alpha(\mu)}{2\pi} \gamma_{\text{ew}} + \frac{\alpha_s(\mu)}{2\pi} \gamma_s \right) \vec{\epsilon}(\mu),$$





# Matching with high-E EFT

Low-E EFT

SMEFT

$$[\epsilon_i = f(\alpha_j)]_{\mu=M_Z}$$

[Cirigliano, MGA, Jenkins '2010;  
Cirigliano, MGA, Graesser '2012]

$$\frac{\delta G_F}{G_F} = 2 [\hat{\alpha}_{\varphi l}^{(3)}]_{11+22} - [\hat{\alpha}_u^{(1)}]_{1221} - 2[\hat{\alpha}_u^{(3)}]_{1122} - \frac{1}{2}(1221),$$

$$V_{1j} \cdot \epsilon_L^{j\ell} = 2 V_{1j} [\hat{\alpha}_{\varphi l}^{(3)}]_{\ell\ell} + 2 [V \hat{\alpha}_{\varphi q}^{(3)}]_{1j} - 2 [V \hat{\alpha}_{lq}^{(3)}]_{\ell\ell 1j},$$

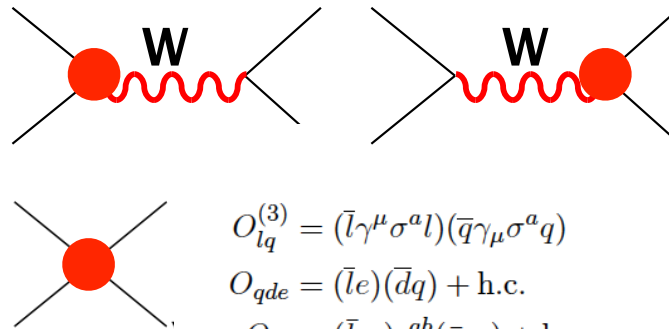
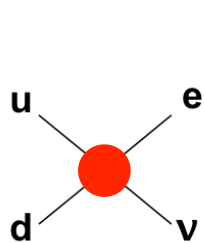
$$V_{1j} \cdot \epsilon_R^j = - [\hat{\alpha}_{\varphi\varphi}]_{1j},$$

$$V_{1j} \cdot \epsilon_{sL}^{j\ell} = - [\hat{\alpha}_{lq}]_{\ell\ell j 1}^*,$$

$$V_{1j} \cdot \epsilon_{sR}^{j\ell} = - [V \hat{\alpha}_{qde}^\dagger]_{\ell\ell 1j},$$

$$V_{1j} \cdot \epsilon_T^{j\ell} = - [\hat{\alpha}_{lq}^t]_{\ell\ell j 1}^*,$$

$$\hat{\alpha} = \alpha \frac{v^2}{\Lambda^2}$$



$$O_{lq}^{(3)} = (\bar{l}\gamma^\mu \sigma^a l)(\bar{q}\gamma_\mu \sigma^a q)$$

$$O_{qde} = (\bar{l}e)(\bar{d}q) + \text{h.c.}$$

$$O_{lq} = (\bar{l}_a e) \epsilon^{ab} (\bar{q}_b u) + \text{h.c.}$$

$$O_{lq}^t = (\bar{l}_a \sigma^{\mu\nu} e) \epsilon^{ab} (\bar{q}_b \sigma_{\mu\nu} u) + \text{h.c.}$$

$$O_{\varphi\varphi} = i(\varphi^T \epsilon D_\mu \varphi)(\bar{u}\gamma^\mu d) + \text{h.c.}$$

$$O_{\varphi q}^{(3)} = i(\varphi^\dagger D^\mu \sigma^a \varphi)(\bar{q}\gamma_\mu \sigma^a q) + \text{h.c.}$$

$$O_{\varphi l}^{(3)} = i(\varphi^\dagger D^\mu \sigma^a \varphi)(\bar{l}\gamma_\mu \sigma^a l) + \text{h.c.}$$

$$O'_{\varphi\varphi} = i(\varphi^T \epsilon D_\mu \varphi)(\bar{\nu}\gamma^\mu e) + \text{h.c.}$$

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Low-E EFT

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[Cirigliano, MGA, Jenkins '2010;  
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$$V_{1j} \cdot \epsilon_R^j = - [\hat{\alpha}_{\varphi\varphi}]_{1j},$$

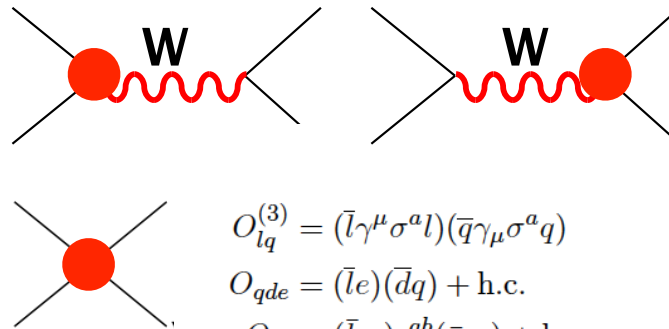
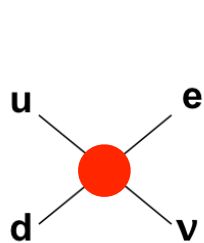
$$V_{1j} \cdot \epsilon_{sL}^{j\ell} = - [\hat{\alpha}_{lq}]_{\ell\ell j 1}^*,$$

$$V_{1j} \cdot \epsilon_{sR}^{j\ell} = - [V \hat{\alpha}_{qde}^\dagger]_{\ell\ell 1j},$$

$$V_{1j} \cdot \epsilon_T^{j\ell} = - [\hat{\alpha}_{lq}^t]_{\ell\ell j 1}^*,$$

$$\hat{\alpha} = \alpha \frac{v^2}{\Lambda^2}$$

Beta decays  
sensitive to a few  
EFT coefficients



$$O_{lq}^{(3)} = (\bar{l}\gamma^\mu \sigma^a l)(\bar{q}\gamma_\mu \sigma^a q)$$

$$O_{qde} = (\bar{l}e)(\bar{d}q) + \text{h.c.}$$

$$O_{lq} = (\bar{l}_a e) \epsilon^{ab} (\bar{q}_b u) + \text{h.c.}$$

$$O_{lq}^t = (\bar{l}_a \sigma^{\mu\nu} e) \epsilon^{ab} (\bar{q}_b \sigma_{\mu\nu} u) + \text{h.c.}$$

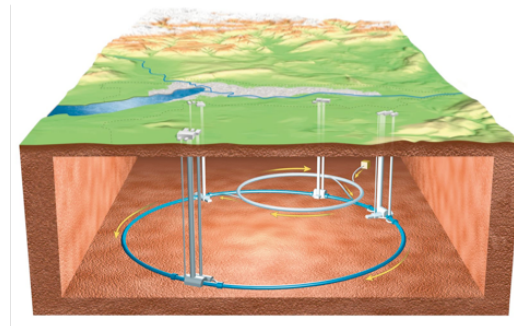
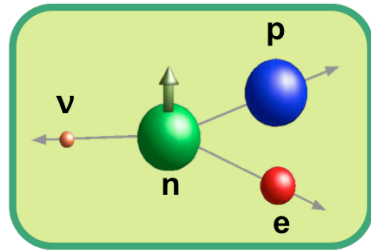
$$O_{\varphi\varphi} = i(\varphi^T \epsilon D_\mu \varphi)(\bar{u}\gamma^\mu d) + \text{h.c.}$$

$$O_{\varphi q}^{(3)} = i(\varphi^\dagger D^\mu \sigma^a \varphi)(\bar{q}\gamma_\mu \sigma^a q) + \text{h.c.}$$

$$O_{\varphi l}^{(3)} = i(\varphi^\dagger D^\mu \sigma^a \varphi)(\bar{l}\gamma_\mu \sigma^a l) + \text{h.c.}$$

$$O'_{\varphi\varphi} = i(\varphi^T \epsilon D_\mu \varphi)(\bar{\nu}\gamma^\mu e) + \text{h.c.}$$

# Scalar & tensor interactions: $b_{\text{Fierz}}$ vs LHC



Models:

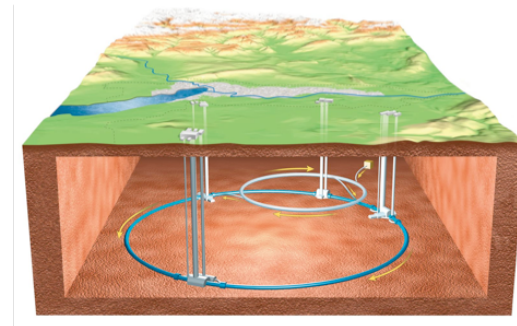
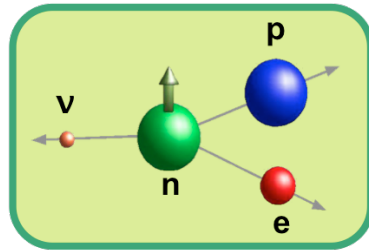
- Tree: RPV-MSSM;

- Loop: RPC-MSSM;

[Herczeg (2001), Profumo et al (2007),  
Yamanaka et al. (2010)]

# Scalar & tensor interactions:

## $b_{\text{Fierz}}$ vs LHC



Models:

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[Herczeg (2001), Profumo et al (2007),  
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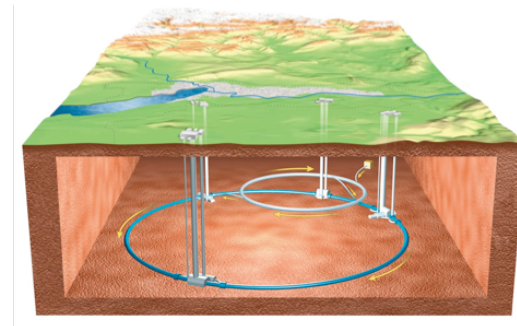
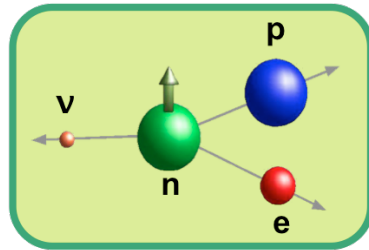
But... Extremely hard to avoid  $\pi \rightarrow l\nu$

- Tree: chiral theories... ( $1 \pm \gamma_5$ )
- Loop: QED & EW mixing (S,T  $\rightarrow$  P)

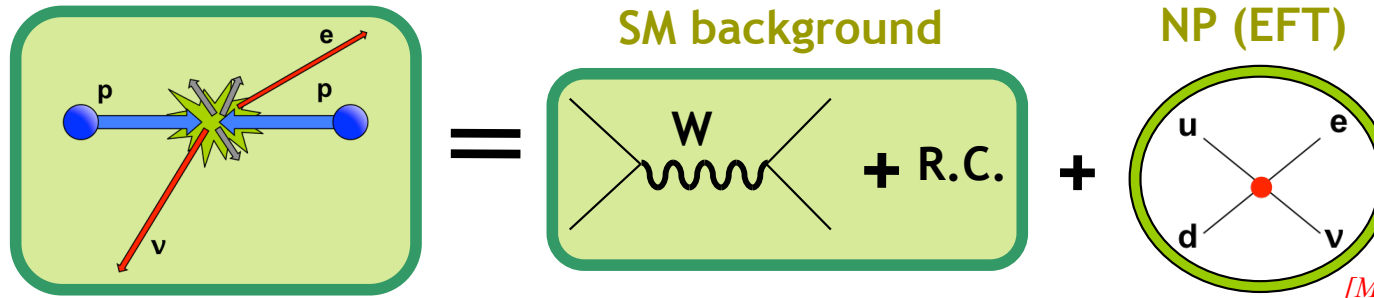
$$|\mathcal{A}(\pi \rightarrow l\nu)|^2 \sim m_l^2 \left( 1 + \frac{M_{QCD}}{m_l} \epsilon_P \right)^2$$

# Scalar & tensor interactions:

## $b_{\text{Fierz}}$ vs LHC



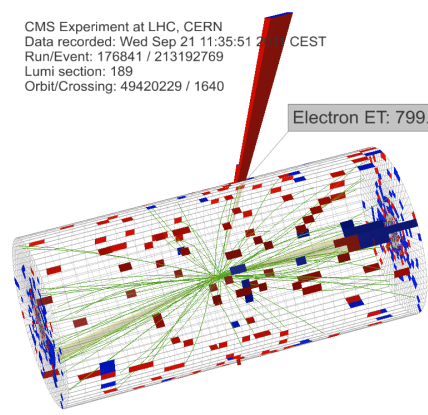
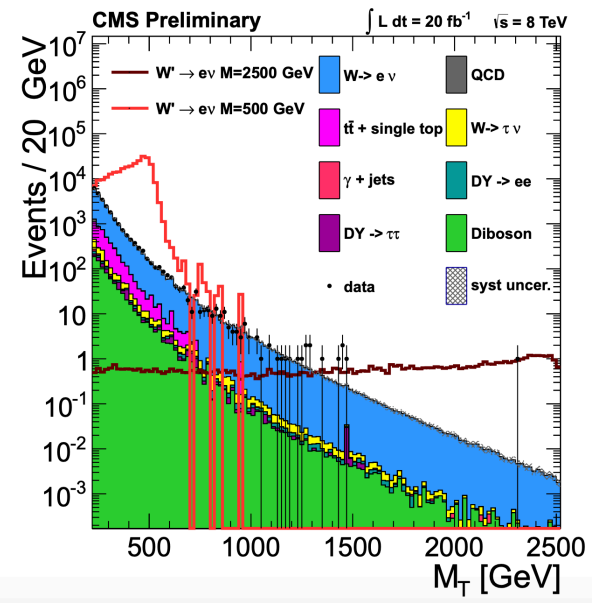
# LHC limits on $\epsilon_{S,T}$



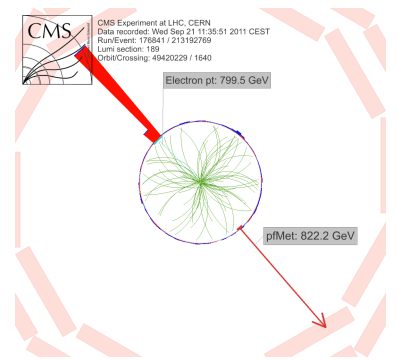
[MGA & Naviliat-Cuncic, Ann. Phys. 525 (2013)]  
 [Cirigliano, MGA & Graesser, JHEP1302 (2013)]  
 [Bhattacharya et al, PRD85 (2012)]

$$N_{pp \rightarrow evX}(m_T^2 > m_{T,cut}^2) = \epsilon \times L \times \sigma_{pp \rightarrow evX}(m_T^2 > m_{T,cut}^2) = \epsilon \times L \times (\sigma_W + \sigma_S \epsilon_S^2 + \sigma_T \epsilon_T^2)$$

(Interference w/ SM  $\sim m/E$ )

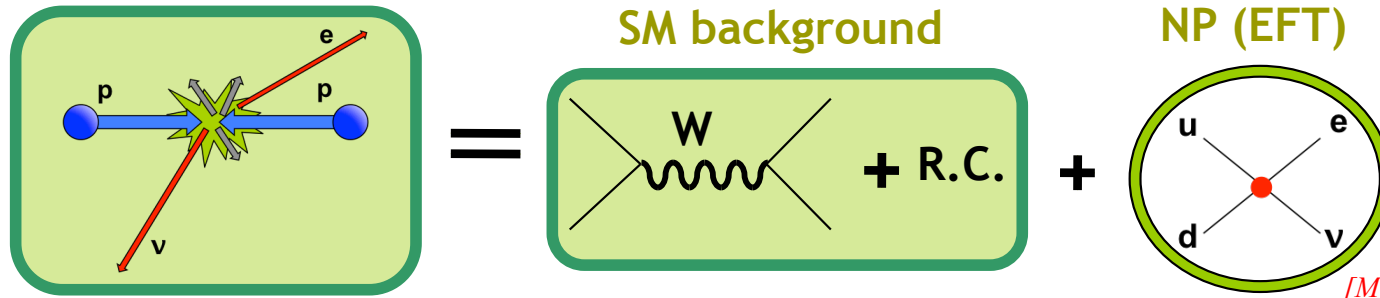


CMS Experiment at LHC, CERN  
 Data recorded: Wed Sep 21 11:35:51 2011 CEST  
 Run/Event: 176841 / 213192769  
 Lumi section: 189  
 Orbit/Crossing: 49420229 / 1640



$$m_T \equiv \sqrt{2E_T^e E_T^\nu (1 - \cos \Delta\phi_{e\nu})}$$

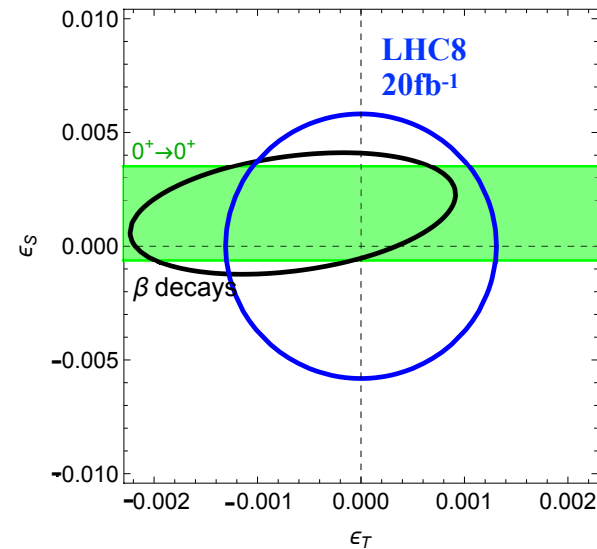
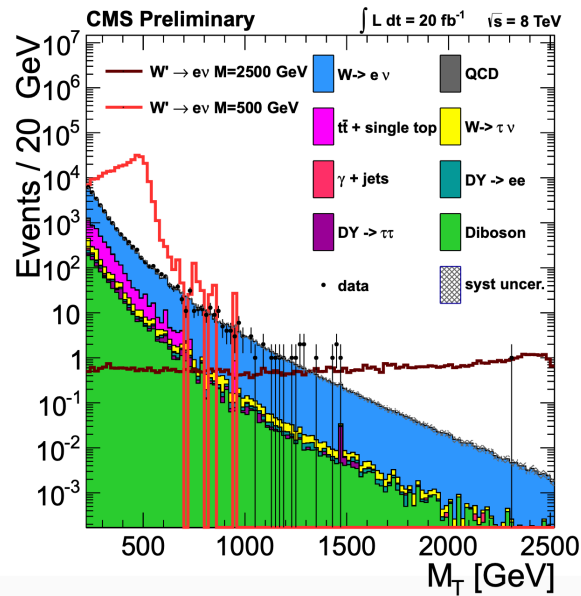
# LHC limits on $\epsilon_{S,T}$



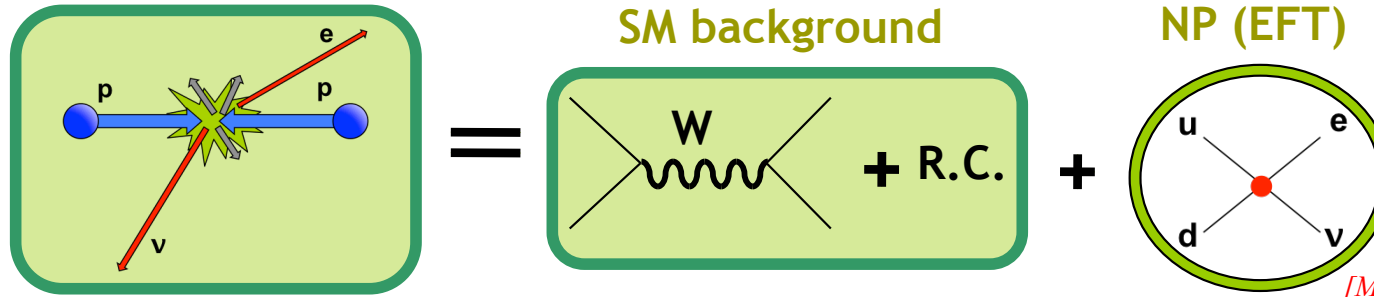
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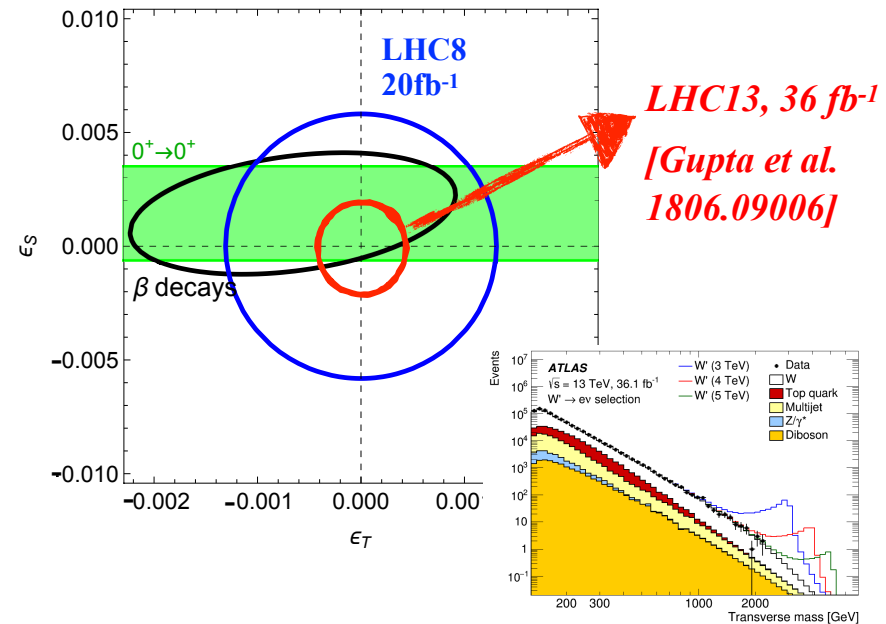
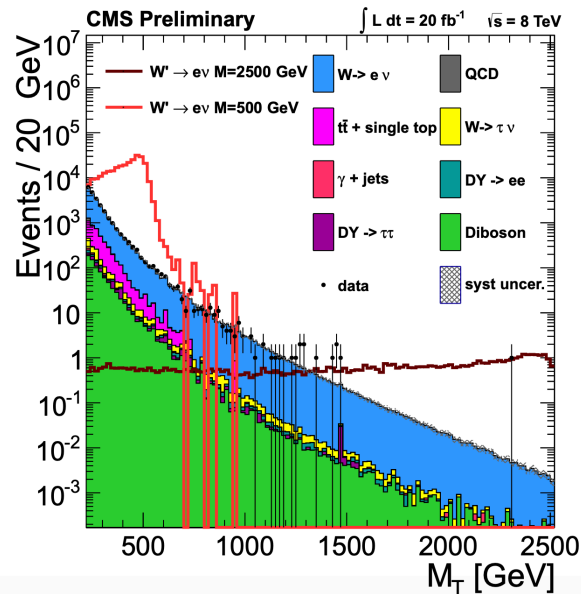
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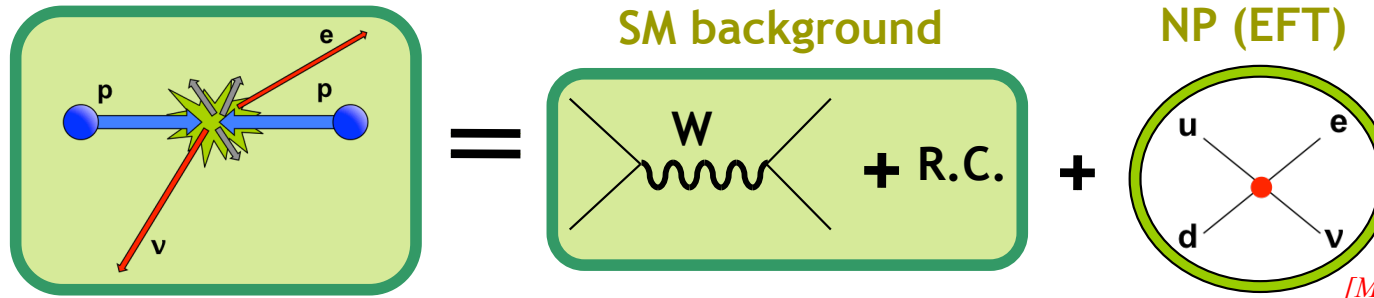
$$N_{pp \rightarrow e\nu X}(m_T^2 > m_{T,cut}^2) = \epsilon \times L \times \sigma_{pp \rightarrow e\nu X}(m_T^2 > m_{T,cut}^2) = \epsilon \times L \times (\sigma_W + \sigma_S \epsilon_S^2 + \sigma_T \epsilon_T^2)$$

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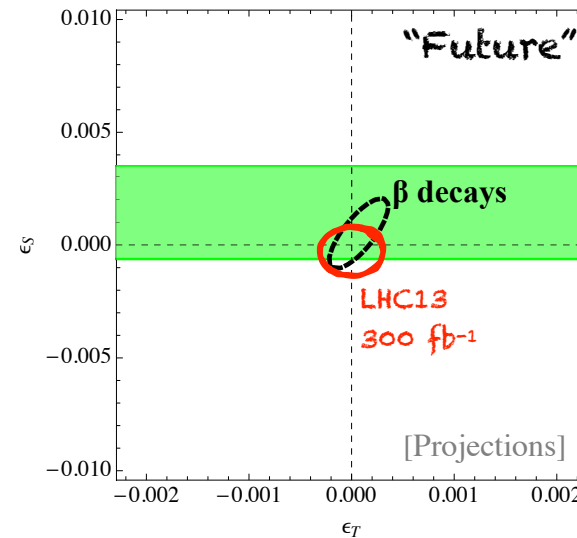
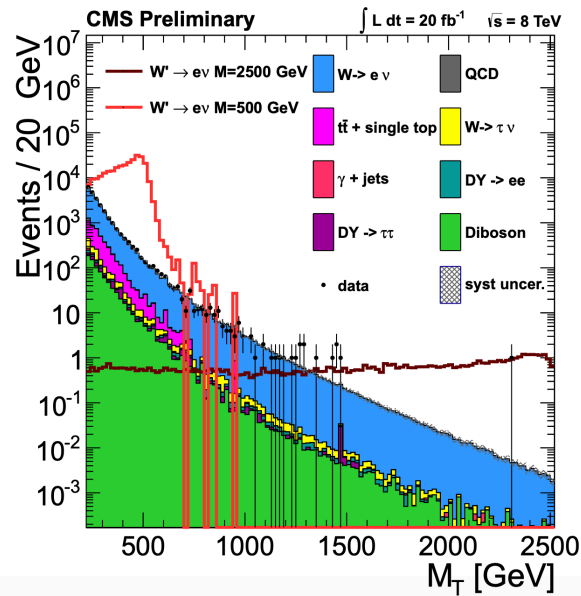
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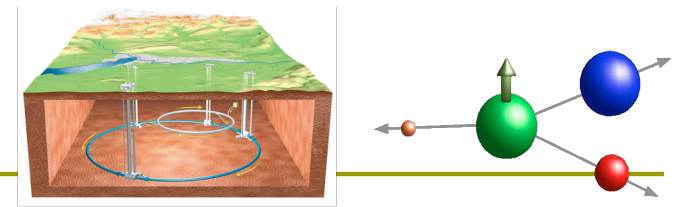
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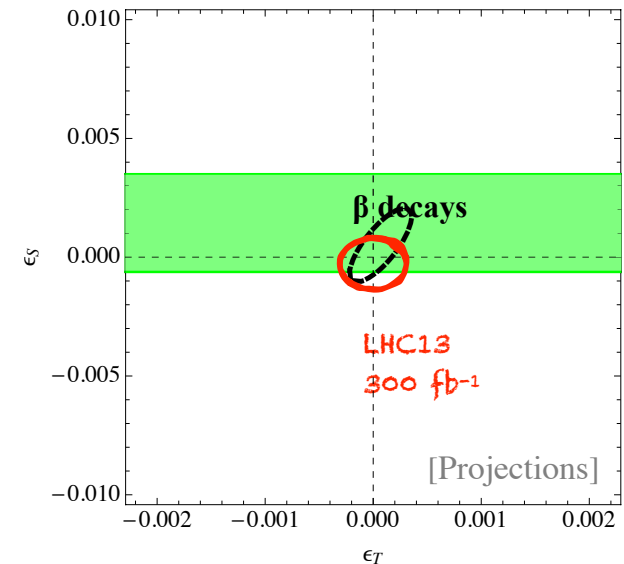
[MGA, O. Naviliat Cuncic, N. Severijns, 1803.08732;  
 Gupta et al. 1806.09006]

# Conclusions



- (Sub) permil-level precision in  $\beta$  decays
  - Great QCD progress
  - Experimental progress too
  - Rad. Corrections?
  
- General EFT analysis available
  - Comparison between  $\beta$ -decay observables;
  - Comparison with APV, LEP, LHC, ...
  - $\beta$  decays are competitive TeV probes;
  
- More (Exp + Th) results expected in the near future

$$\begin{pmatrix} |C_V| \\ C_A/C_V \\ C_S/C_V \\ C_T/C_A \end{pmatrix} = \begin{pmatrix} 0.98595(34) G_F/\sqrt{2} \\ -1.2728(17) \\ 0.0014(12) \\ 0.0020(22) \end{pmatrix}$$



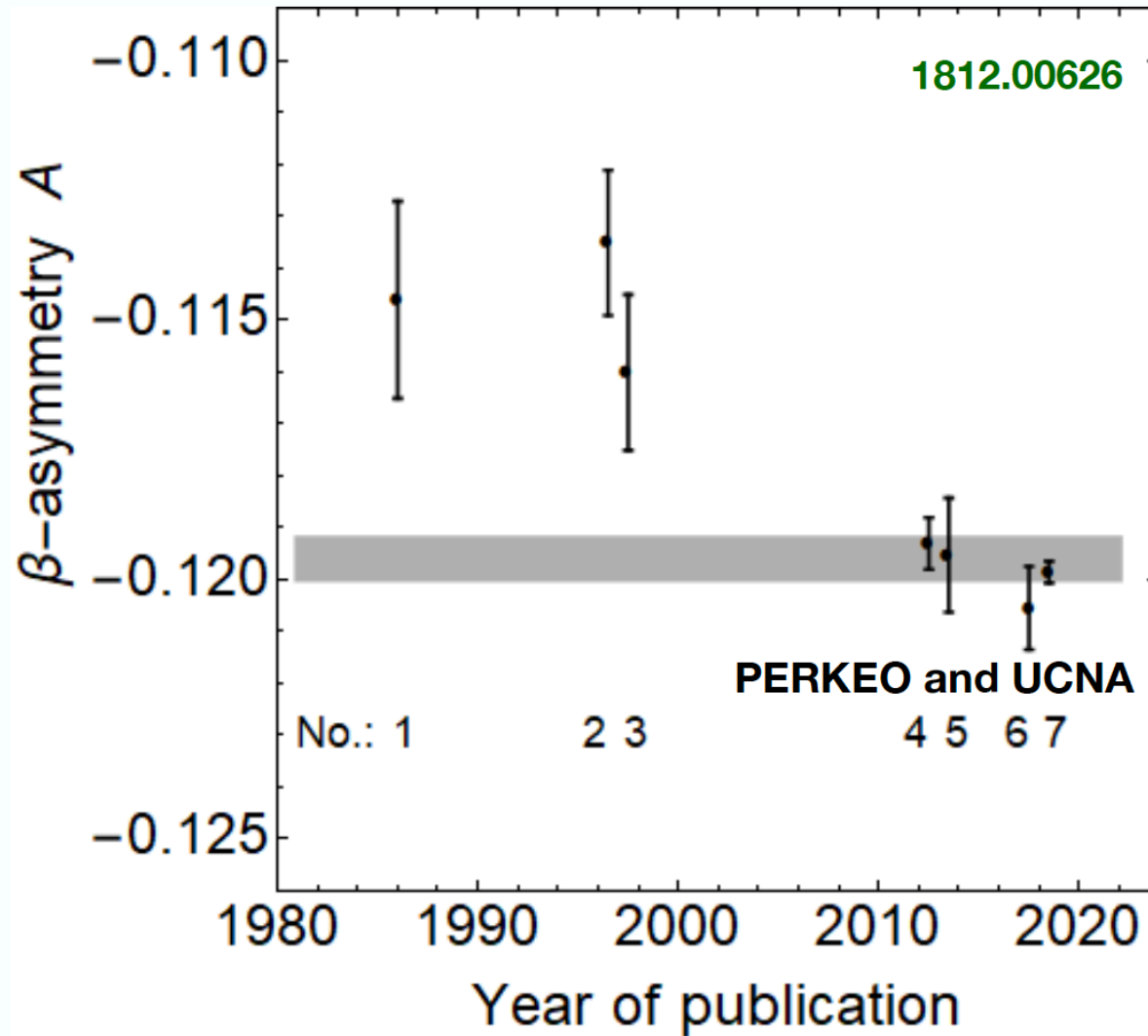
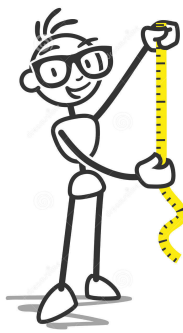
$$\frac{\alpha_6^{(i)}}{\Lambda^2} = f_i(g_{NP}, M_{NP})$$

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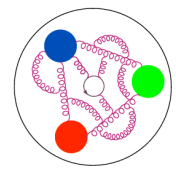
# Backup slides

# Neutron beta asymmetry

Precision:  
0(0.01 - 1)% !!



# From hadrons to quarks



Likewise...

[MGA & Martin Camalich,  
Phys. Rev. Lett. 112 (2014)]

$$\partial_\mu (\bar{u}\gamma^\mu\gamma_5 d) = i(m_d + m_u)\bar{u}\gamma_5 d \quad \longrightarrow \quad g_P = \frac{M_n + M_p}{m_d + m_u} g_A = 348(11)$$

Implications? It almost compensates the bilinear suppression!

$$\langle p(p_p) | \bar{u}\gamma_5 d | n(p_n) \rangle = g_P(q^2) \bar{u}_p(p_p) \gamma_5 u_n(p_n) \sim q/M \sim 10^{-3}$$

“since the nucleons are treated nonrelativistically, the pseudoscalar couplings are omitted”

[Jackson, Treiman & Wyld, 1957]

The same  $\beta$  decay experiments that set bounds on  $S$  &  $T$ , are also sensitive to  $P$ !

$$\langle b \frac{m}{E} \rangle \approx 0.23\epsilon_S - 3.45\epsilon_T - 0.03\epsilon_P$$

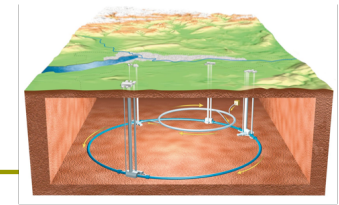
From current data:

$$\epsilon_P = -0.08(15) \text{ (90\%CL)}$$

But... the bounds on  $\epsilon_P$  from pion decays are much stronger!!!

$$|\mathcal{A}(\pi \rightarrow \ell\nu)|^2 \sim m_\ell^2 \left( 1 + \frac{M_{QCD}}{m_\ell} \epsilon_P \right)^2$$

# If we see a bump...

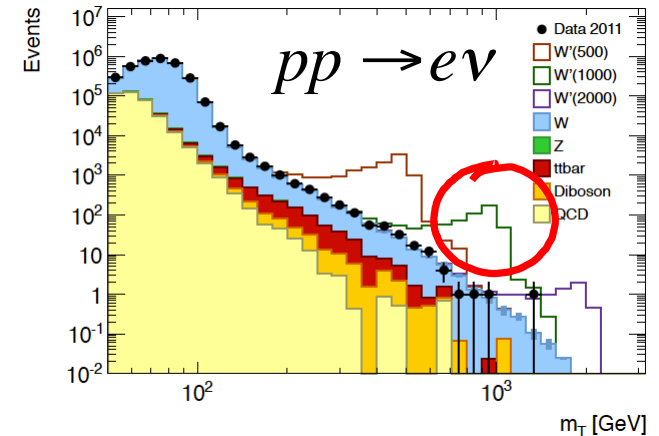
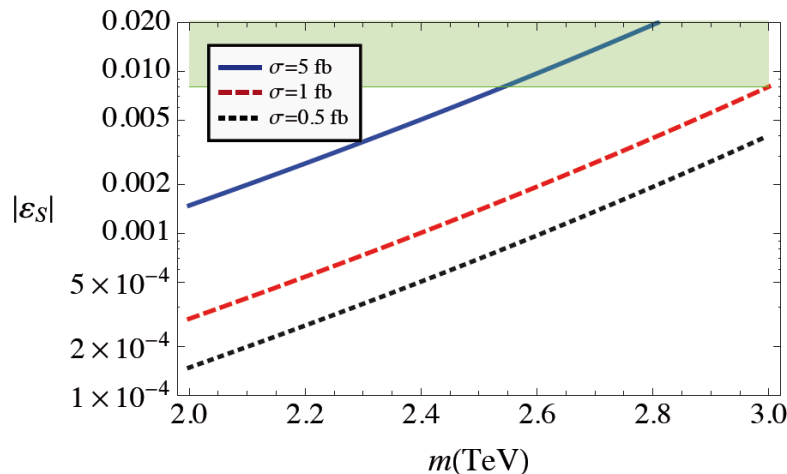


- EFT breaks down...  
Toy model: scalar resonance:

$$\mathcal{L} = \lambda_S V_{ud} \phi^+ \bar{u}d + \lambda_l \phi^- \bar{e} P_L \nu_e$$

- Then we have a lower-limit value for  $\epsilon_S$ :

$$\sigma \cdot \text{BR} \leq \frac{|V_{ud}|}{12v^2} \frac{\pi}{\sqrt{2N_c}} |\epsilon_S| \tau L(\tau)$$



$$L(\tau) = \int_{\tau}^1 dx f_q(x) f_q'(\tau/x) / x$$

$$\tau = m^2 / s$$

$$\epsilon_S = 2\lambda_S \lambda_l \frac{v^2}{m^2}$$

**Nice interplay of two experiments separated for so many orders of magnitudes!!!!**

[T. Battacharya et al., 2012]